



# Electron Lens cookbook

Recipies from simulations

V. Previtali, A. Valishev  
G. Stancari, I. Morozov, D. Shatilov

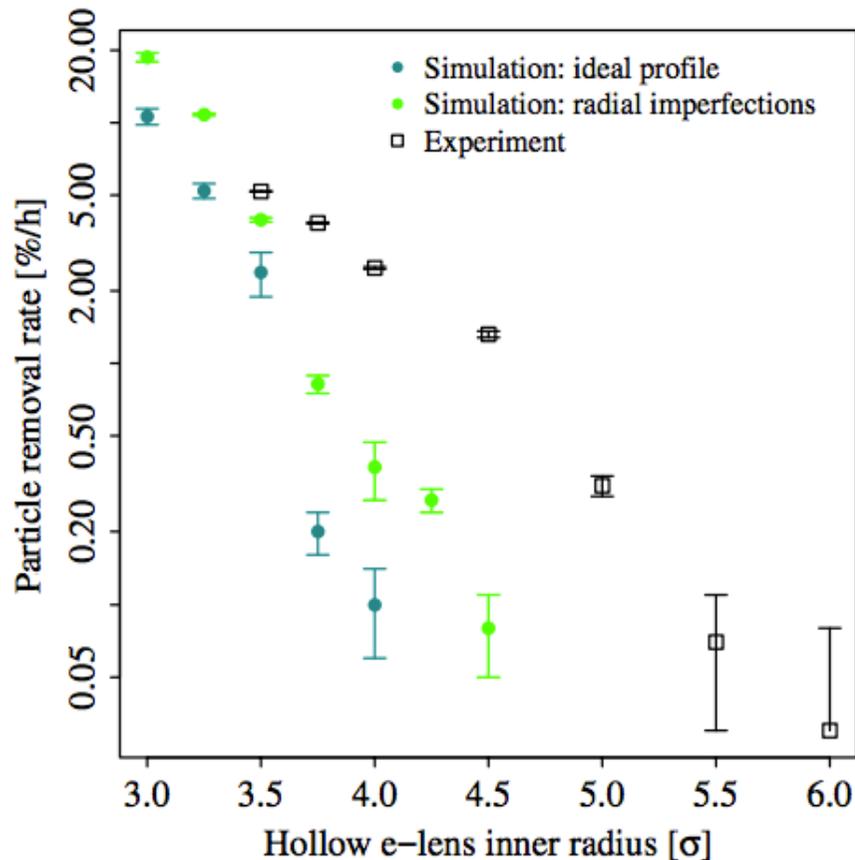
Thanks for the helpful discussions with  
S. Redaelli, B. Salvachua Ferrando, A. Rossi

# Goal: can we use the available hardware for meaningful beam tests at the LHC and SPS?



- past experience at Tevatron shows promising results
- Extrapolation of the e-lens effect on the LHC / SPS beam is not straightforward. Simulations are required.
- Preliminary question: what is the actual status of the simulations? is it possible to have a realistic evaluation from simulations?
  - past simulations at FNAL with Lifetrack
- New simulations for LHC with Sixtrack.
  - **scraping time** (how fast can we remove the particle halo?)
  - what are the side effects?
- Does it make sense to test the device in the SPS first?

# Tevatron simulations



Simulations performed with Lifetrack (code benchmarked with Sixtrack).

Tevatron pbar beam in collision.

Elens model including e-beam profile imperfections

Summary of Tevatron experimental results:

1. halo removal rate **reproduced within a factor 2-5**
2. core not affected **qualitatively reproduced**



# Sixtrack simulations: the ingredients

## The beam

- 7 TeV beam 1
- Purely H or V halo between 4 and 6 sigma, no off-momentum
- no diffusion (the halo is not replenished)
- 6400 particles, 200K turns (standard jobs)

## The machine: a quasi linear approximation

- thin nominal LHC optics, **no collision**
- linear machine + sextupoles

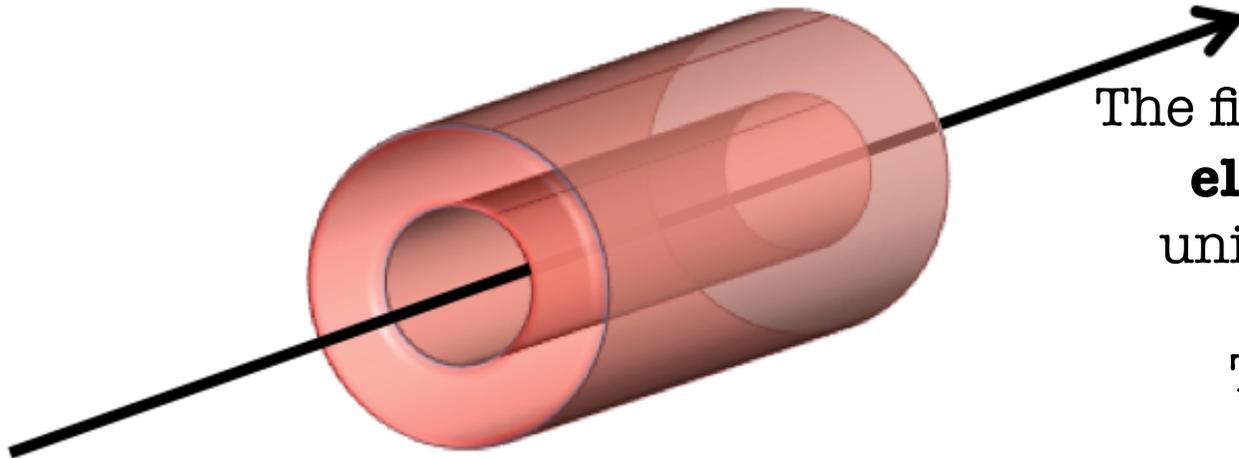
## A minimal LHC collimation system

name	angle[rad]	betax[m]	betay[m]	halfgap[m]	Material	Length[m]	sigx[m]	sigy[m]
ELENS.TRY.1	0.00000E+00	0.18181E+03	0.17991E+03	0.12092E-02	C	0.20000E+01	0.30230E-03	0.30072E-03
TCP.D6L7.B1	0.15710E+01	0.15887E+03	0.78263E+02	0.13130E-01	C	0.60000E+00	0.28259E-03	0.19834E-03
TCP.C6L7.B1	0.00000E+00	0.15053E+03	0.82763E+02	0.18210E-01	C	0.60000E+00	0.27507E-03	0.20396E-03

- Only the e-lens with two primary collimators in IP7 at 6.2 sigma
- the beam is round at the e-lens location (1 sigma about 300 um)
- electron lens in IP4 (see integration talk)
- typical parameters for the electron lens , as used in Tevatron (current 1.2 A, extraction voltage 5 KeV), inner radius 4 sigma

# The hollow e-lens: a first model

Charge distribution



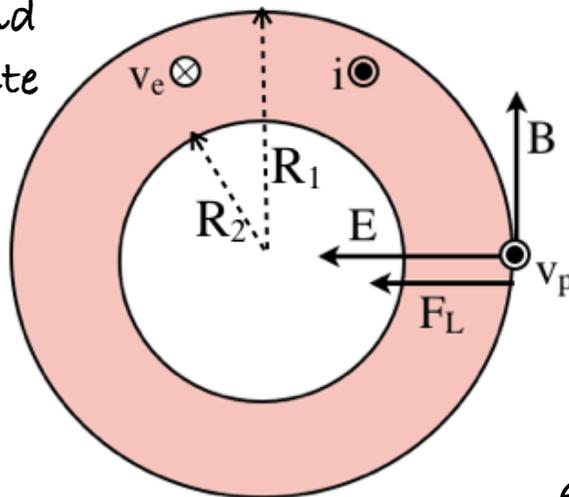
The first model is **the perfect elens**: hollow cylinder  
uniform current density

Total current 1.2 A

Electric and Magnetic fields

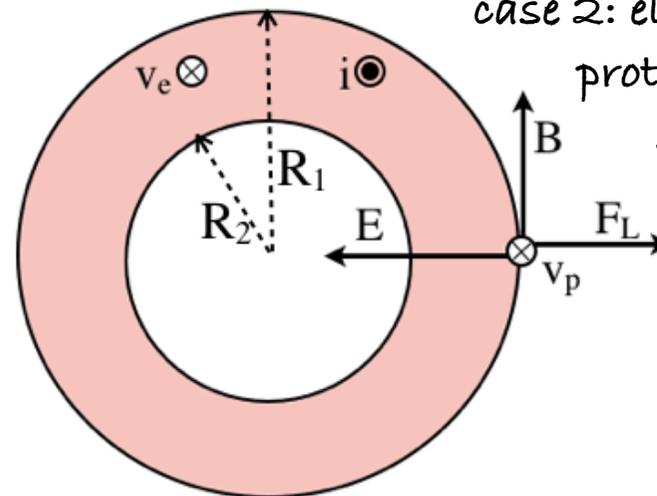
case 1: electrons and  
protons have opposite  
versus

desired  
configuration:  
e.m. forces  
add up



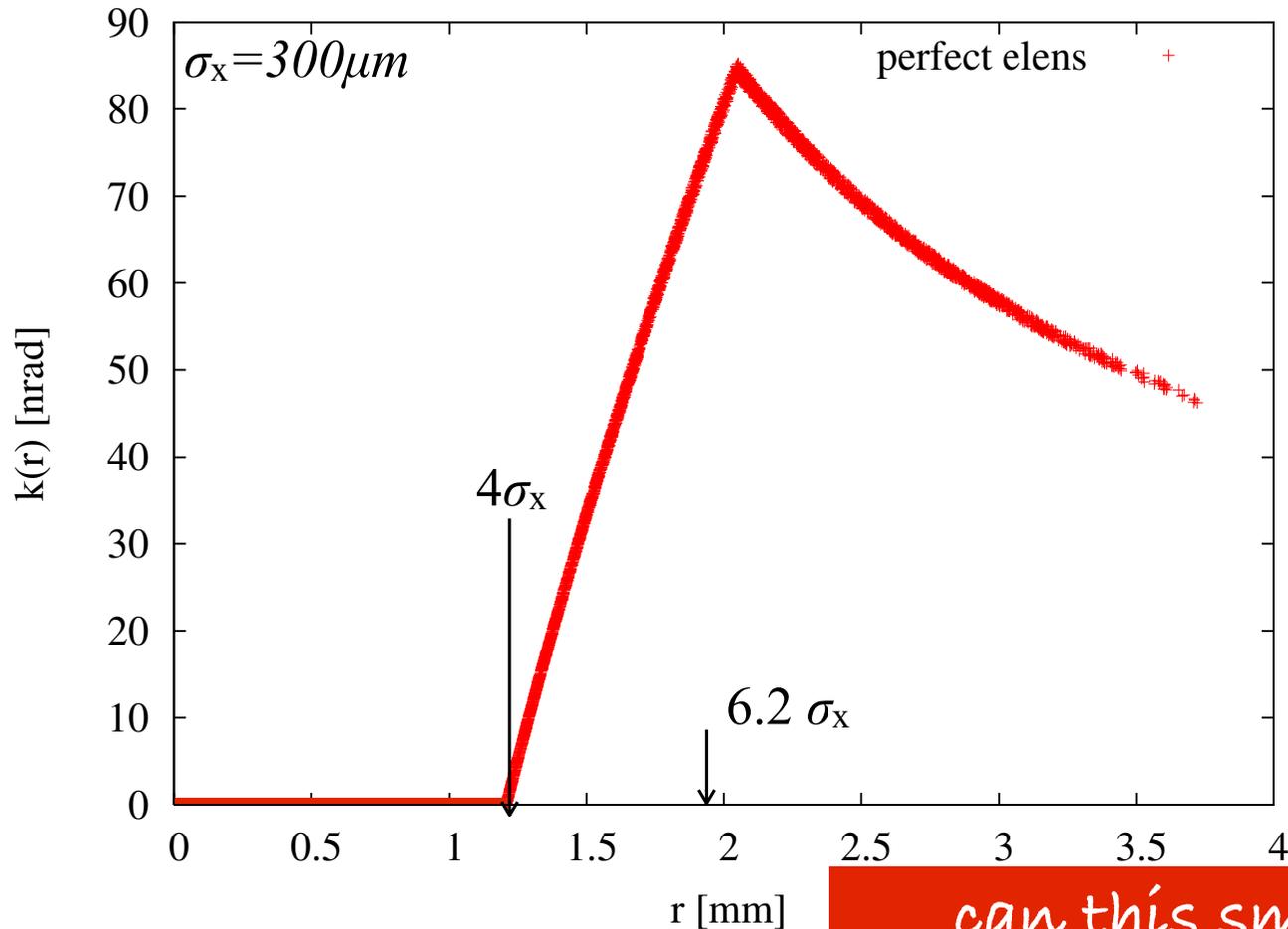
6

case 2: electrons and  
protons have the  
same versus



# The perfect e-lens: the nominal kick

Highly non linear field, focusing in both planes. For symmetry reasons,  $F=0$  within the electron lens inner radius.

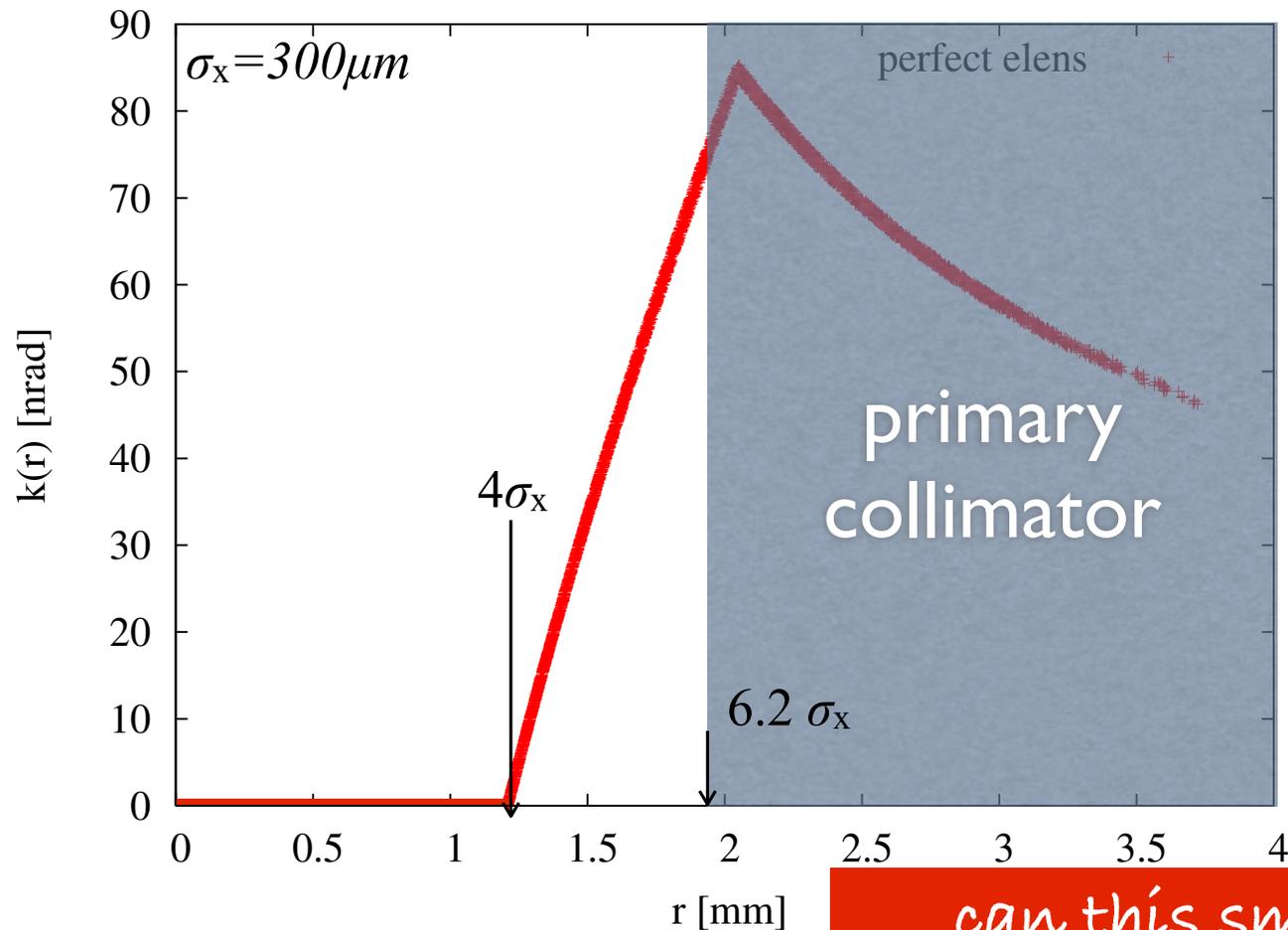


maximum kick value for 7 TeV  
of the order of  $10^2$  nrad  
(about 1% of sigma)

can this small kick be  
efficient for scraping the 7  
TeV LHC halo?

# The perfect e-lens: the nominal kick

Highly non linear field, focusing in both planes. For symmetry reasons,  $F=0$  within the electron lens inner radius.



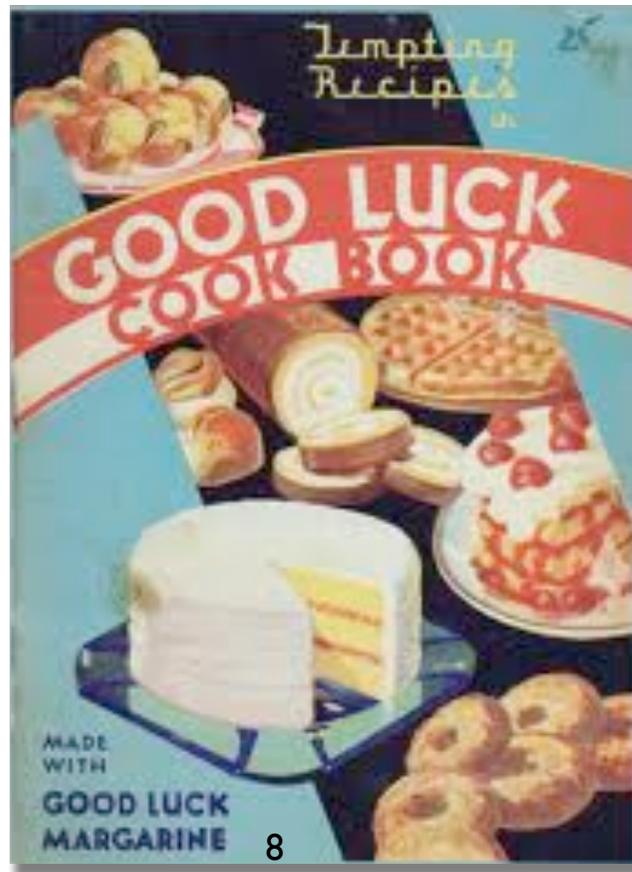
maximum kick value for 7 TeV  
of the order of  $10^2$  nrad  
(about 1% of sigma)

can this small kick be  
efficient for scraping the 7  
TeV LHC halo?

can this small kick be  
efficient for scraping  
the 7 TeV LHC halo?



Yes, but you need to know how to use it

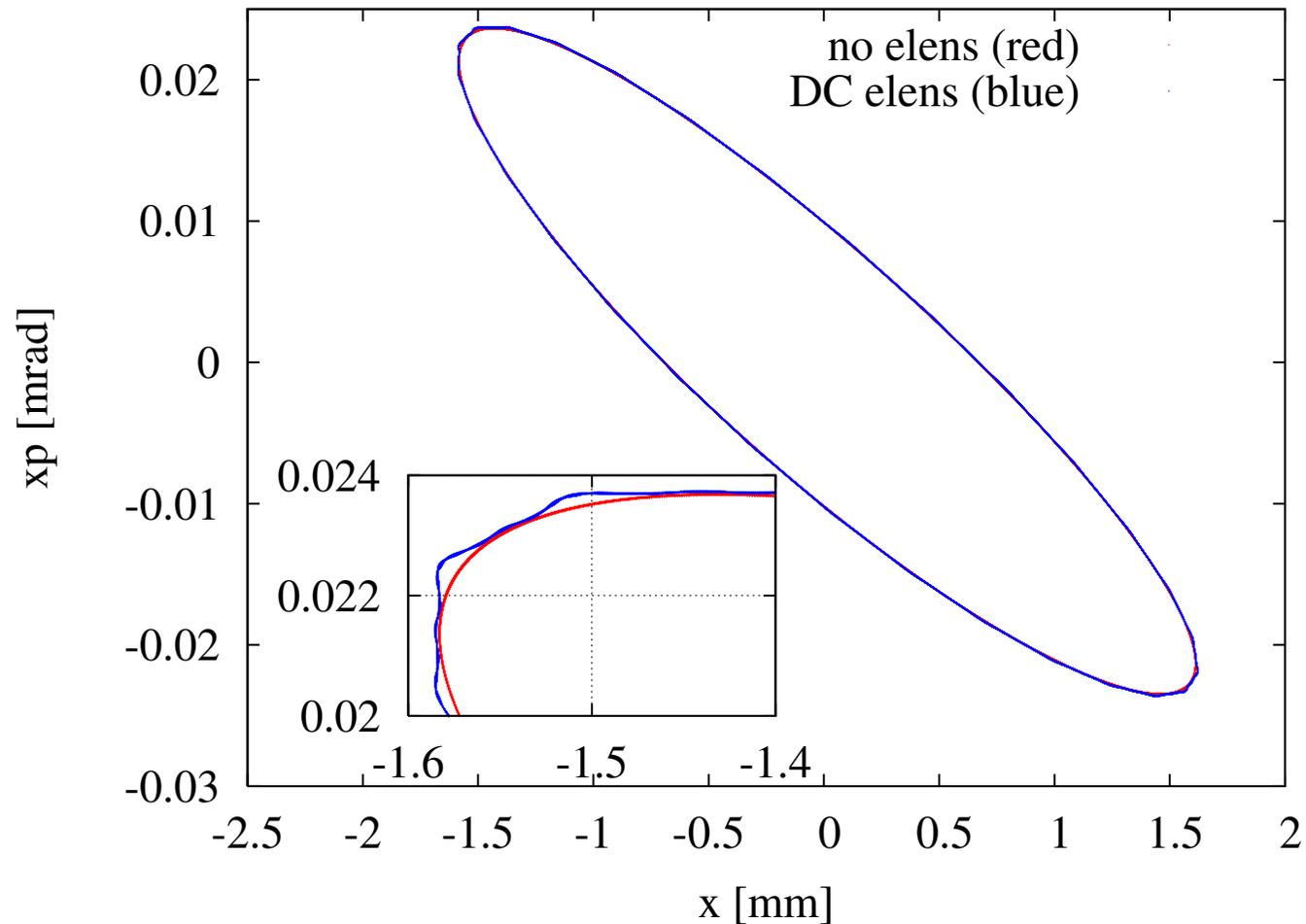


# 4 basic recipes



1. **DC mode:** e-lens is always ON
2. **AC mode:** e-lens switched on-off in resonance with the particle transverse motion
3. **random mode:** e-lens is randomly switched on-off turn by turn (coin toss!)
4. **harmonic mode:** e-lens is switched on every  $n$  turns (tevatron mode), simulations in progress

# 1. DC mode: e-lens is always ON



1. mild effect on the phase space
2. induces a small tune shift
3. negligible tune jitter ( $< 1e-5$ )

DC mode is not effective for  
scraping in a linear machine

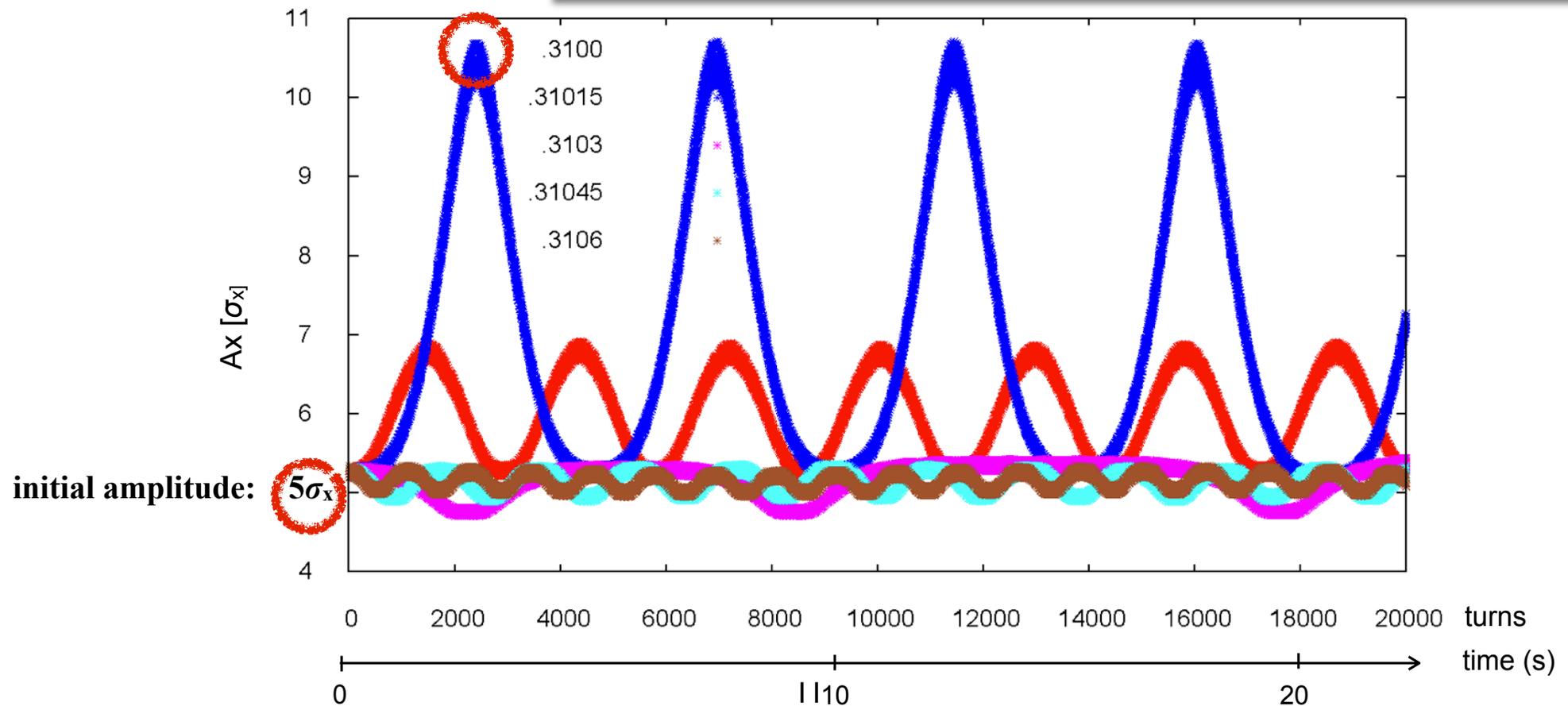
## 2. AC mode: e-lens switched on-off in resonance with the particle oscillation



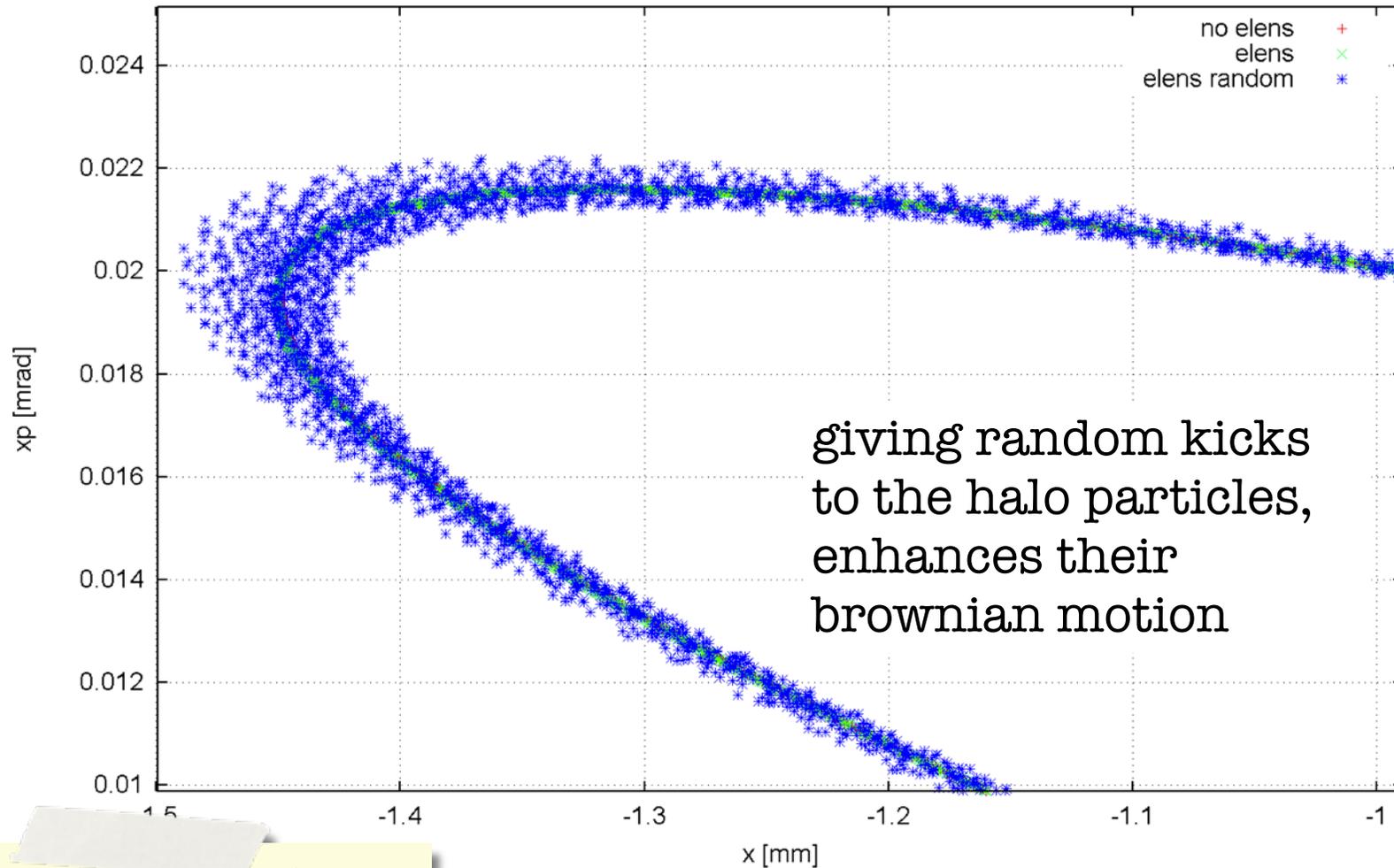
response of the particle to different AC frequencies

with the good frequency, AC mode induces large amplitude oscillations which quickly drive the particles on the collimator

to  $11\sigma_x$  in 2 sec!



### 3. random mode: e-lens is randomly switched on-off turn by turn



random mode  
increases diffusion.

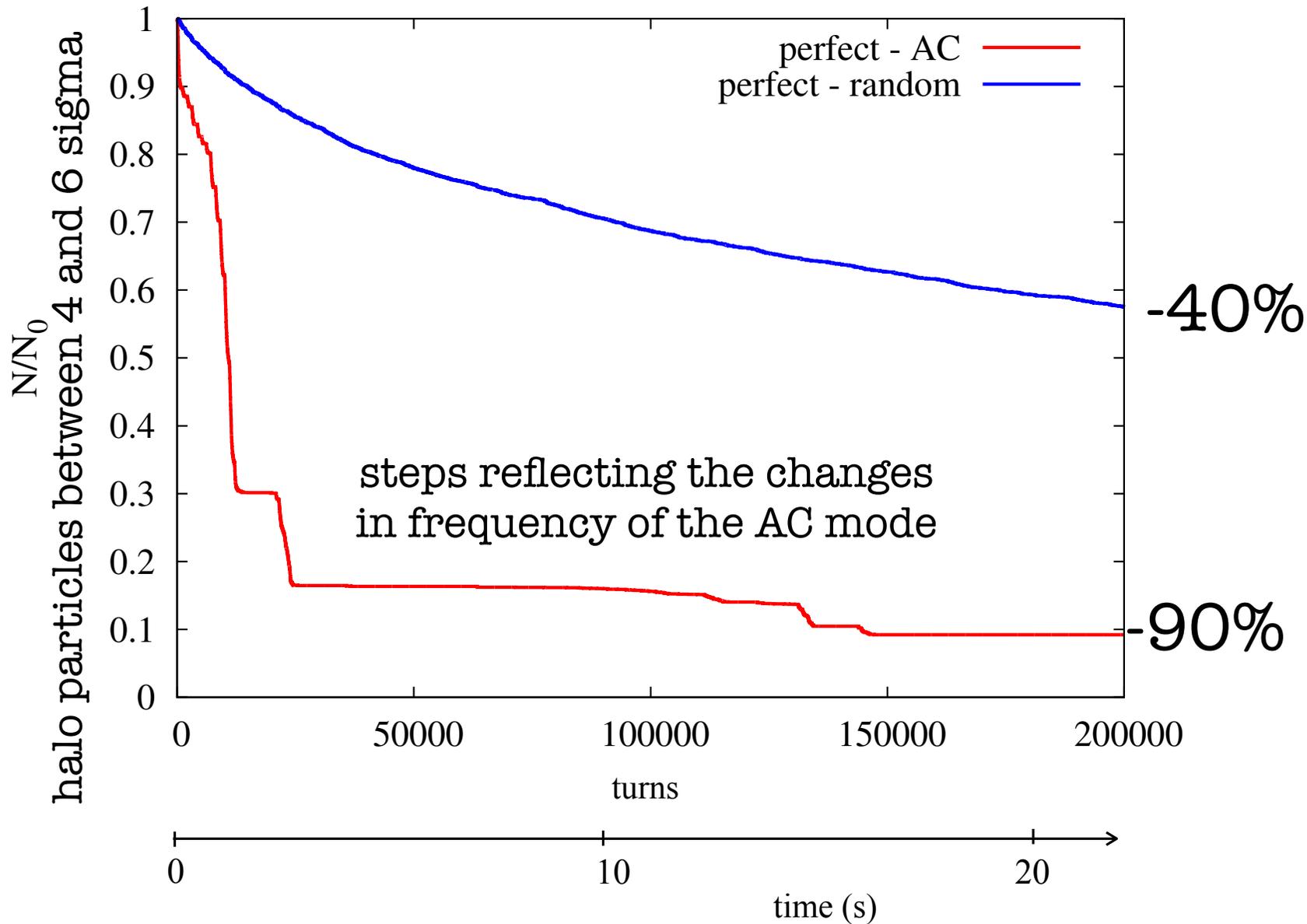
# 4 basic recipes



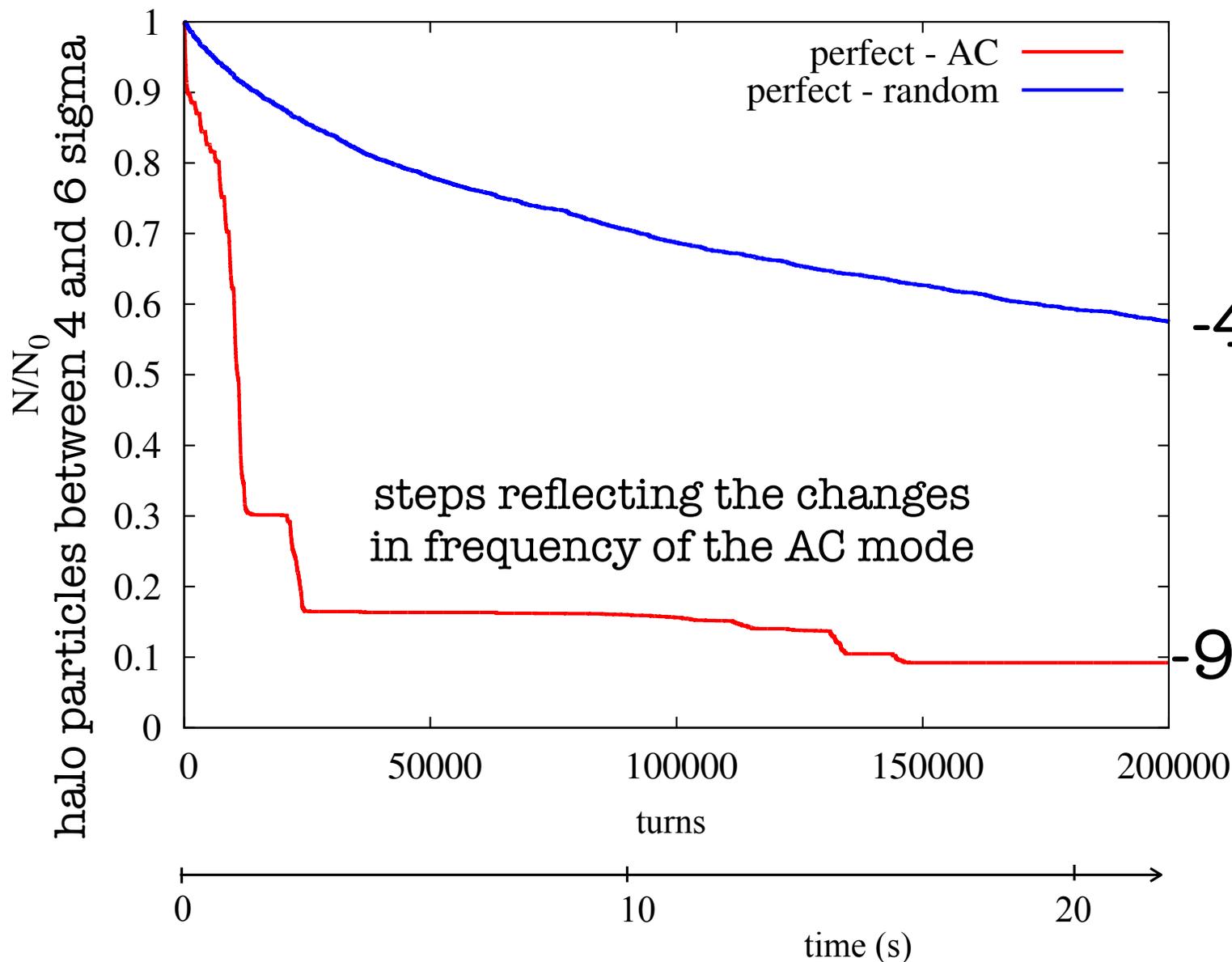
1. **DC mode:** ~~e lens is always ON~~
2. **AC mode:** e-lens switched on-off in resonance with the particle transverse motion
3. **random mode:** e-lens is randomly switched on-off turn by turn (coin toss!)
4. **harmonic mode:** e-lens is switched on every n turns (tevatron mode), simulations in progress

*which mode for what?*

# which mode for what?



# which mode for what?



-40%



slow-cooking

-90%



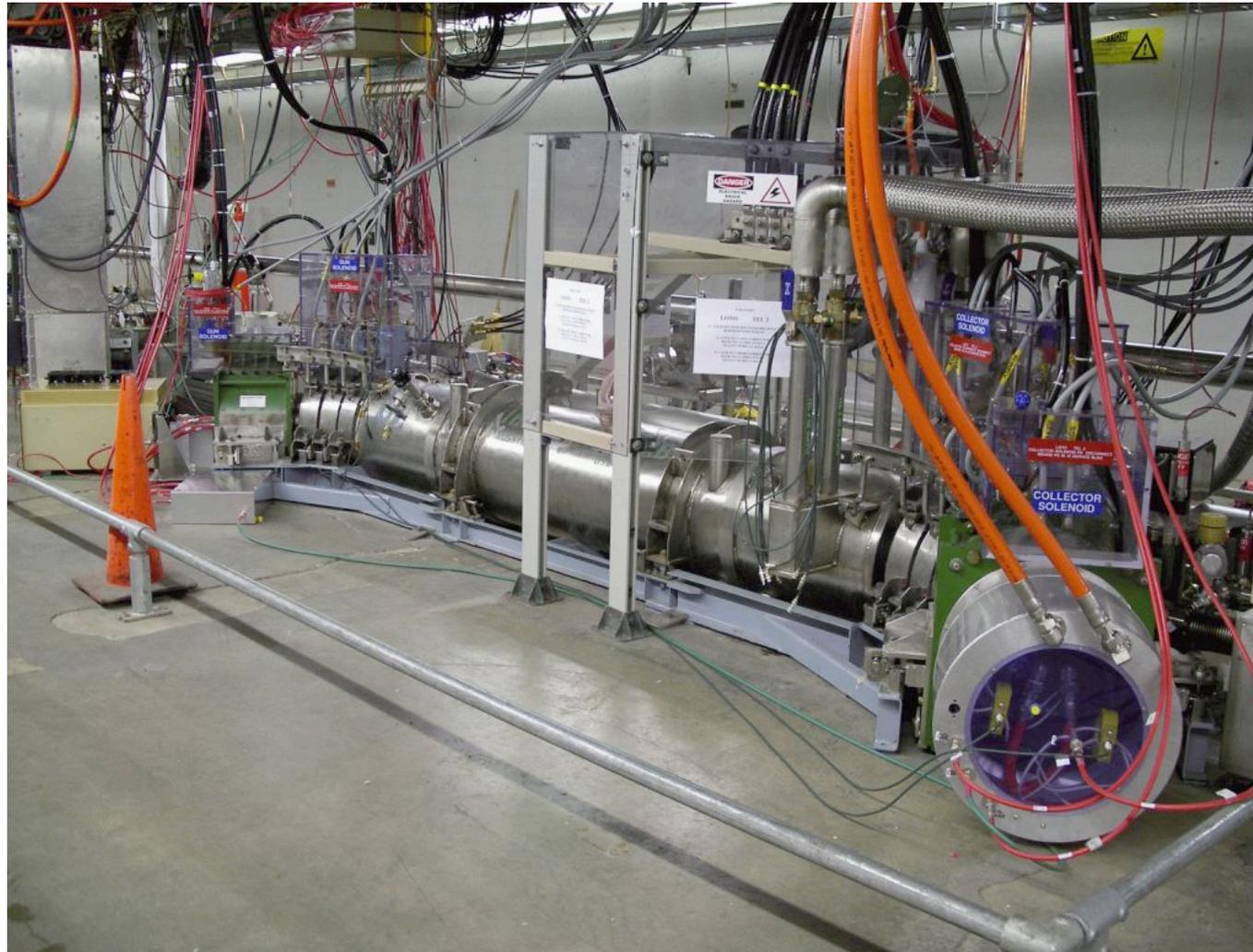
frying pan

(unfortunately?)  
Real life is complicated...

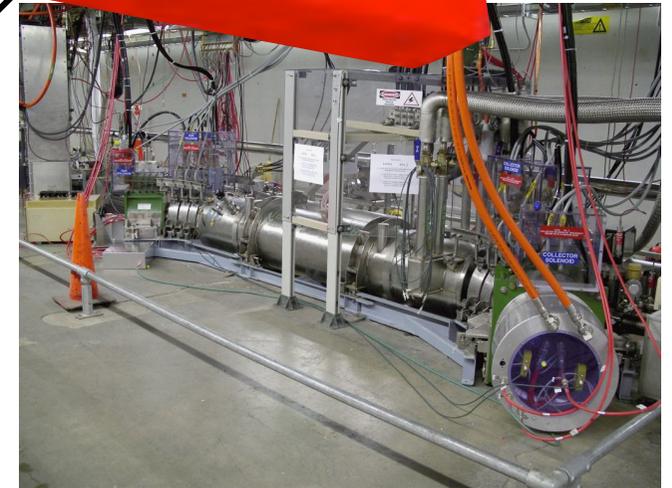
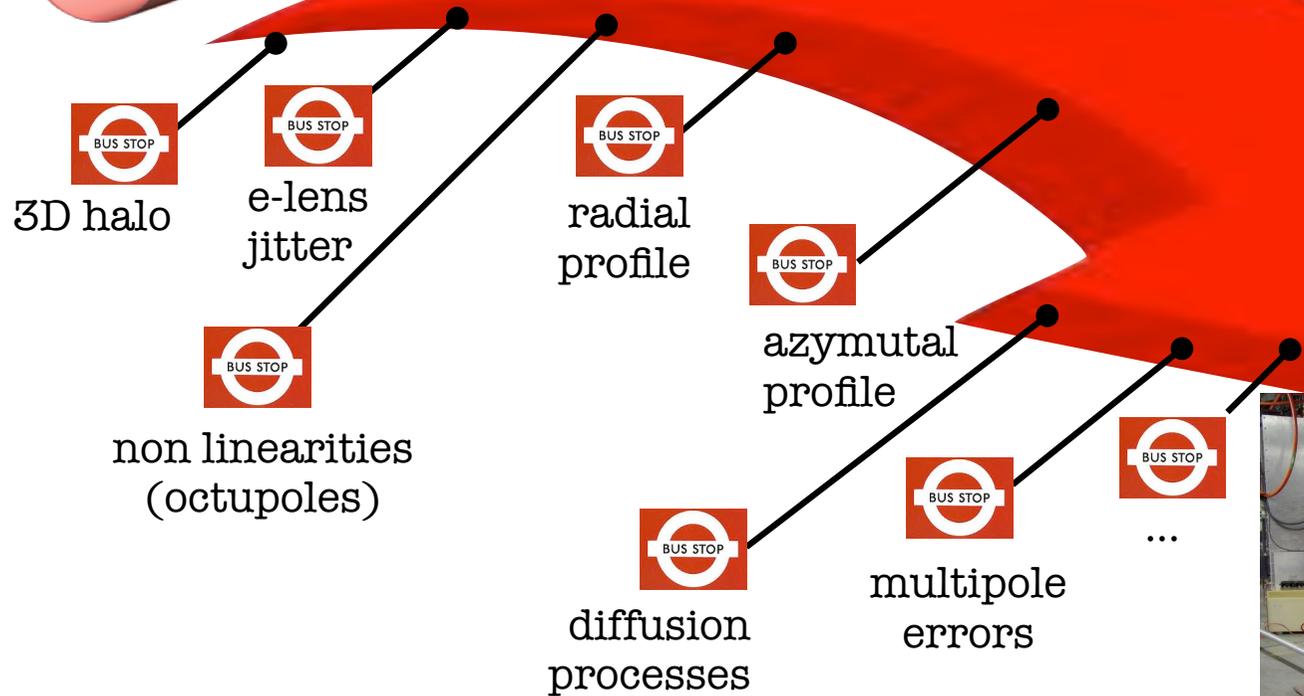
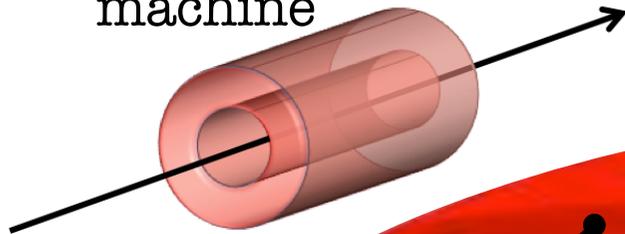


©Prawny Vintage \* [www.ClipartOf.com/1112529](http://www.ClipartOf.com/1112529)

(unfortunately?)  
Real life is complicated...



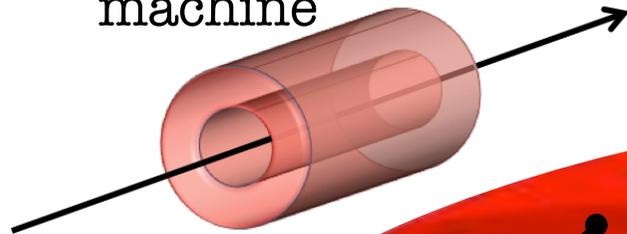
Perfect e-lens in  
quasi-linear  
machine



It's a long (infinite?) way, which may requires many intermediate stops

Real e-lens in real machine

Perfect e-lens in  
quasi-linear  
machine



Today!

  
3D halo

  
e-lens  
jitter

  
radial  
profile

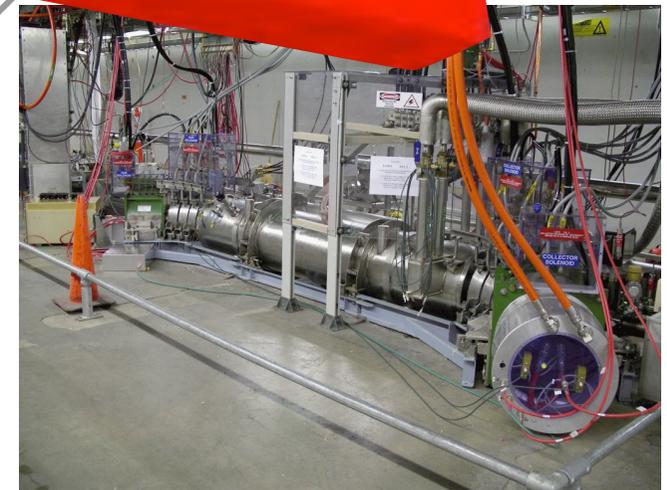
  
azymutal  
profile

  
non linearities  
(octupoles)

  
diffusion  
processes

  
multipole  
errors

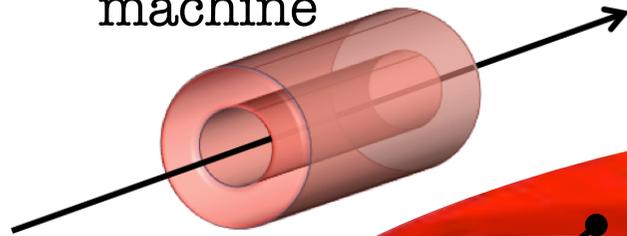
  
...



It's a long (infinite?) way, which may  
requires many intermediate stops

Real e-lens in real machine

Perfect e-lens in  
quasi-linear  
machine



Today!

  
3D halo

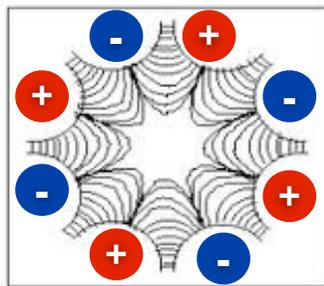
  
e-lens  
jitter

  
radial  
profile

  
azymutal  
profile



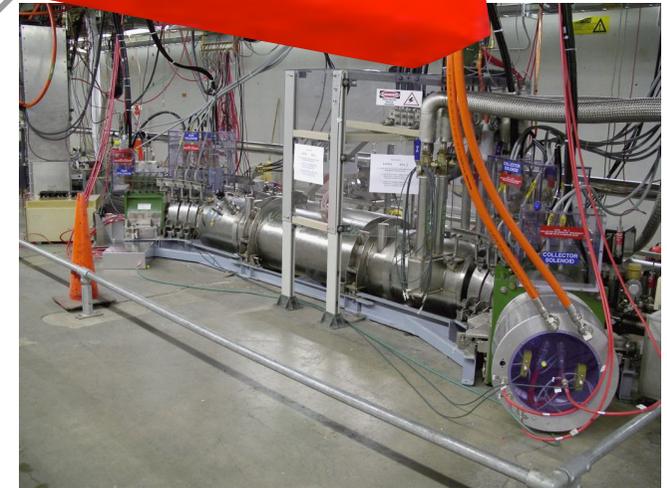
**non linearities  
(octupoles)**



  
diffusion  
processes

  
multipole  
errors

  
...

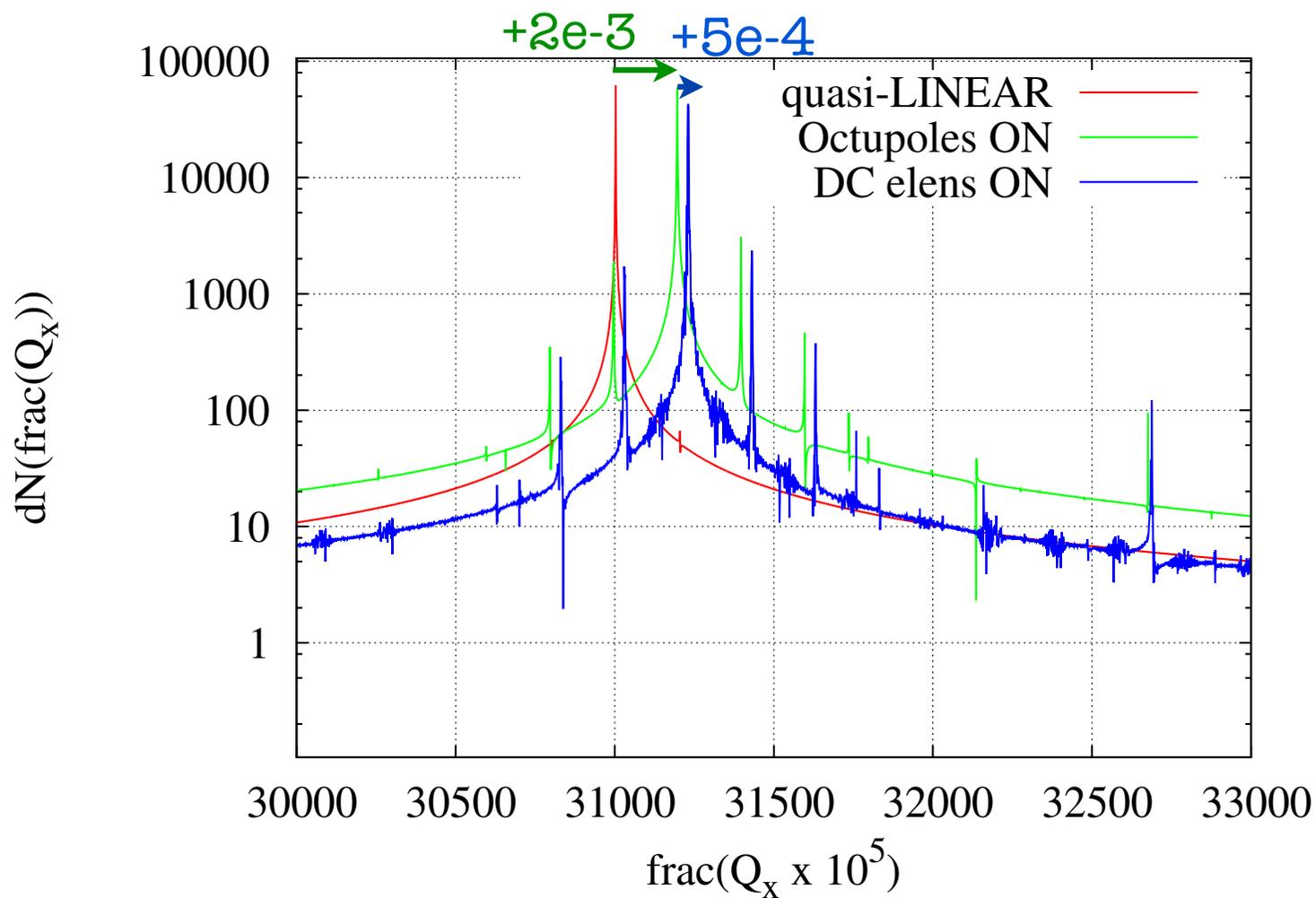
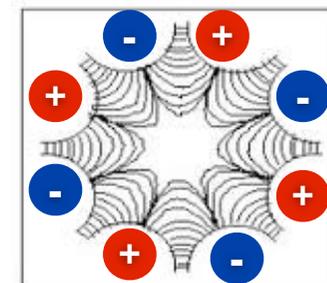


It's a long (infinite?) way, which may  
requires many intermediate stops

Real e-lens in real machine



**non linearities  
(octupoles)**

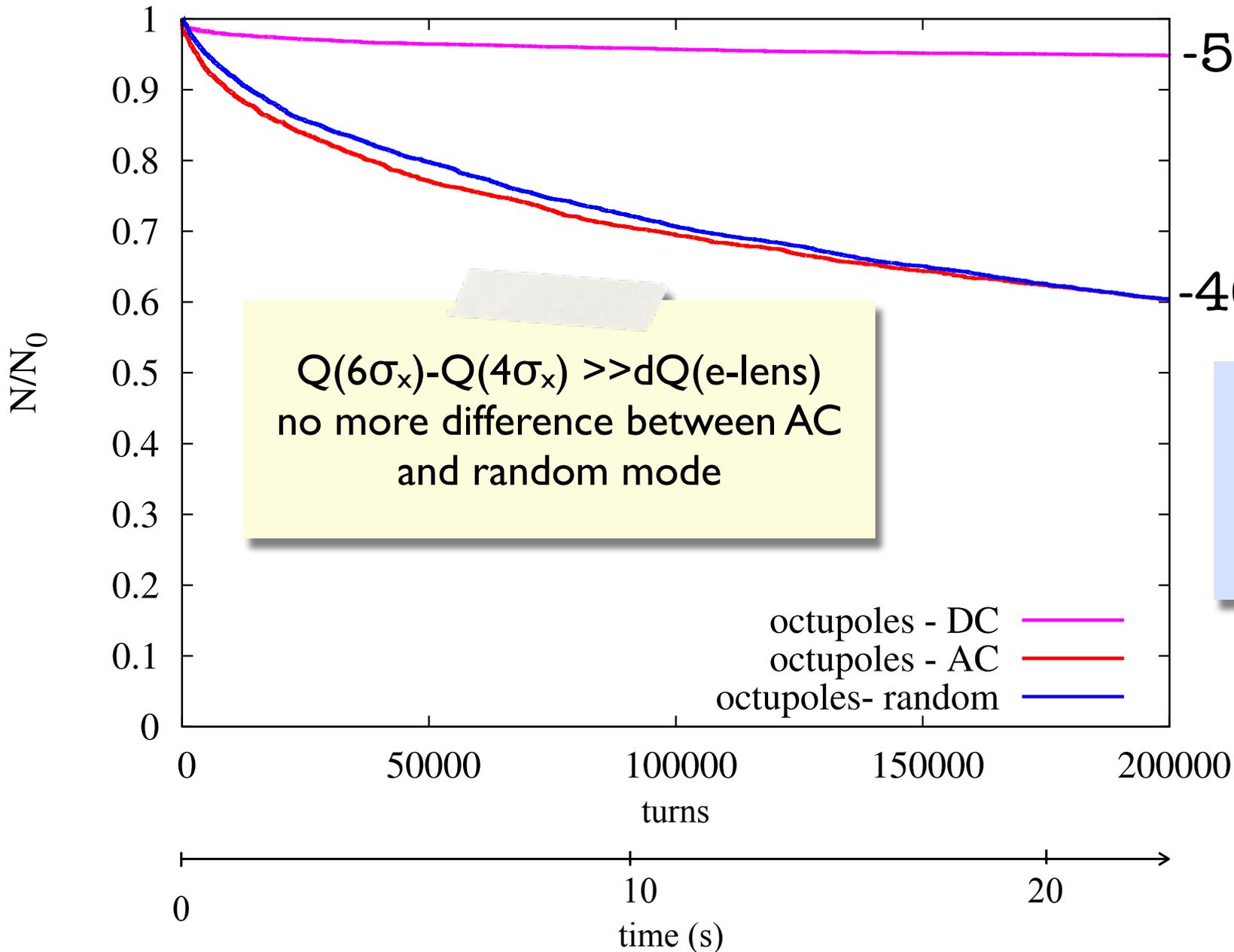
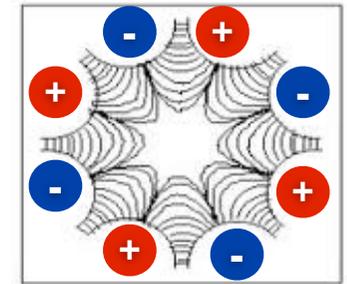


$$Q(6\sigma_x) - Q(4\sigma_x) \sim 1.5e-3$$
$$dQ(\text{e-lens}) \sim 5e-4$$

DC mode start to act as a smooth scraper



non linearities (octupoles)



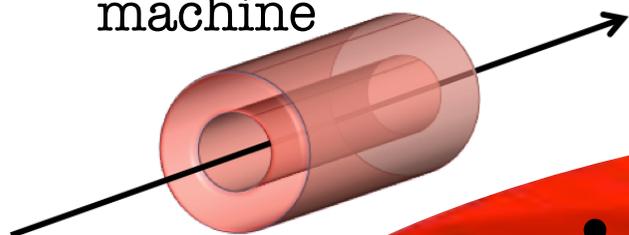
-5%

-40%

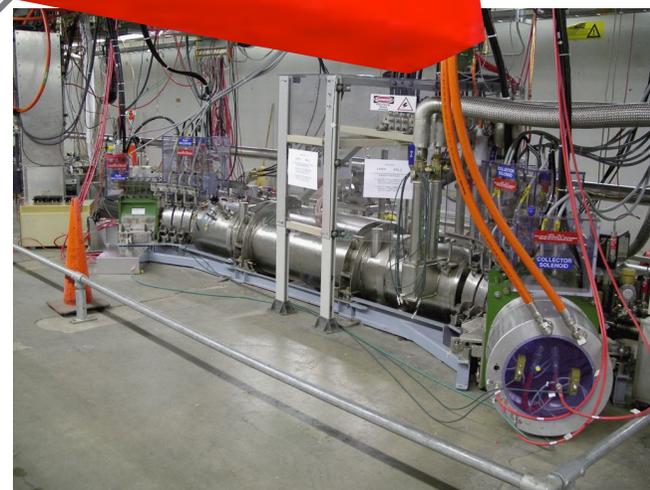
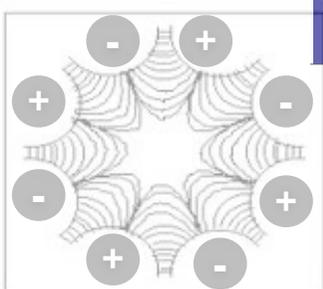
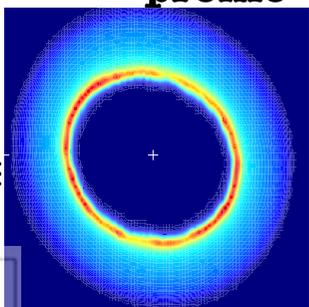
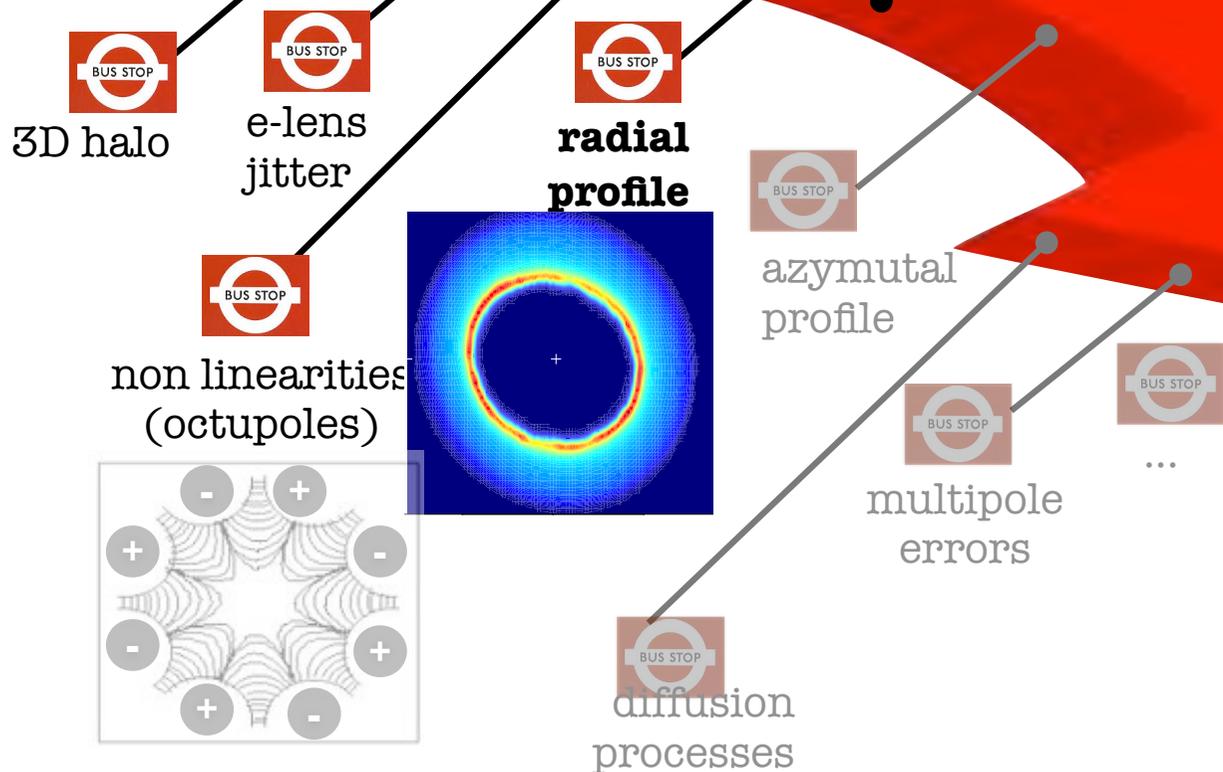
$Q(6\sigma_x) - Q(4\sigma_x) \gg dQ(e\text{-lens})$   
no more difference between AC and random mode

random mode is very robust  
results are unchanged.

Perfect e-lens in  
quasi-linear  
machine



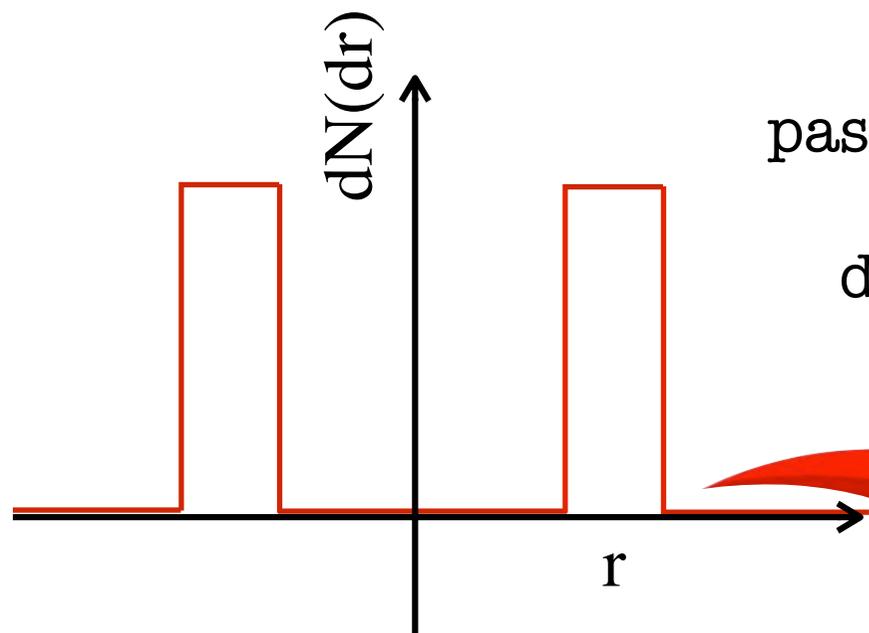
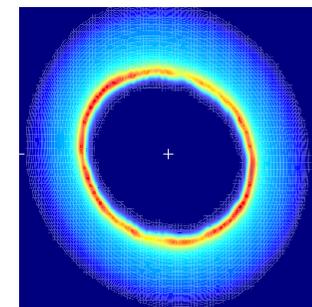
Today!



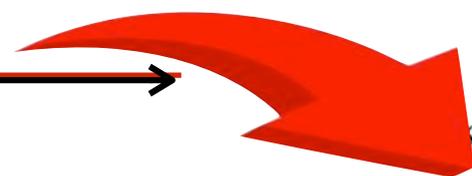
Real e-lens in real machine



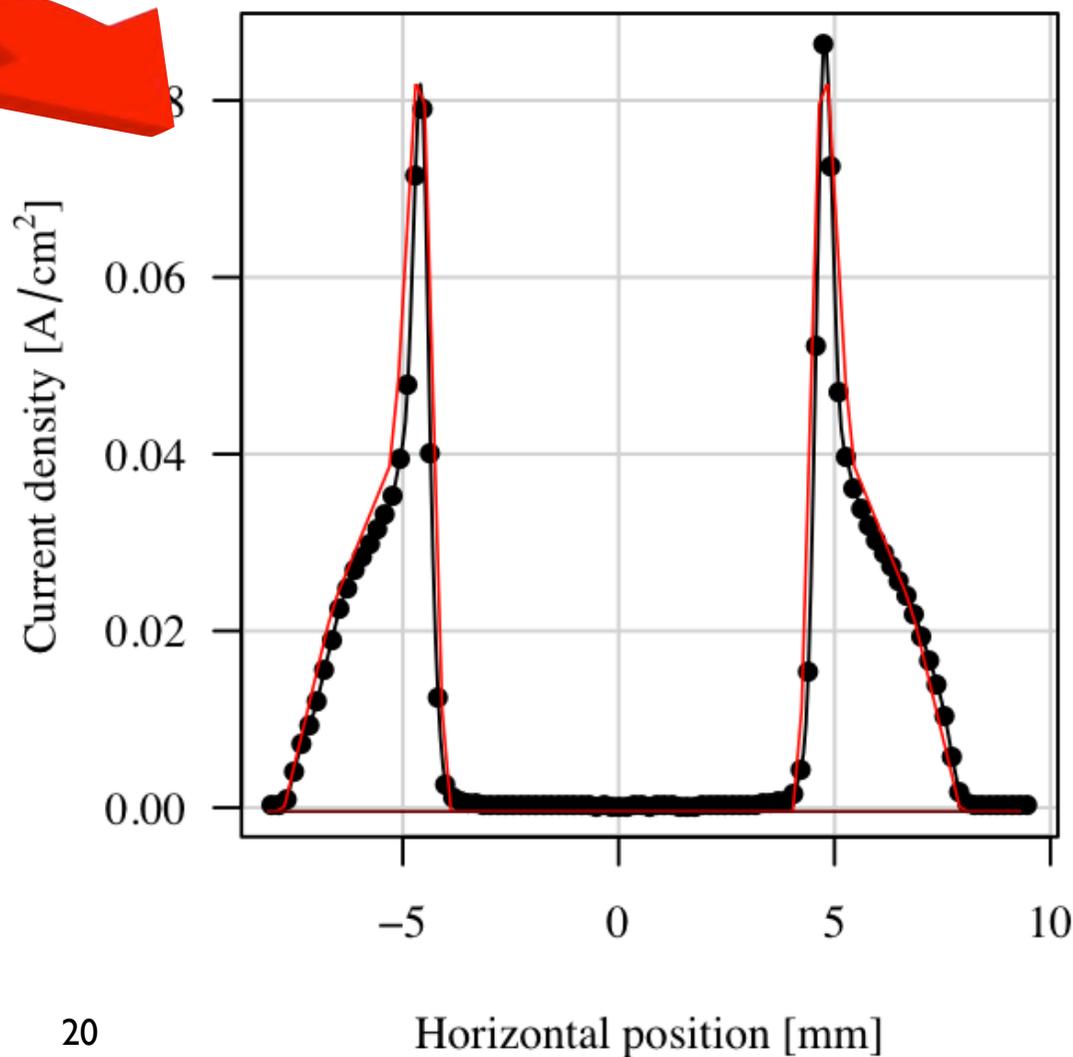
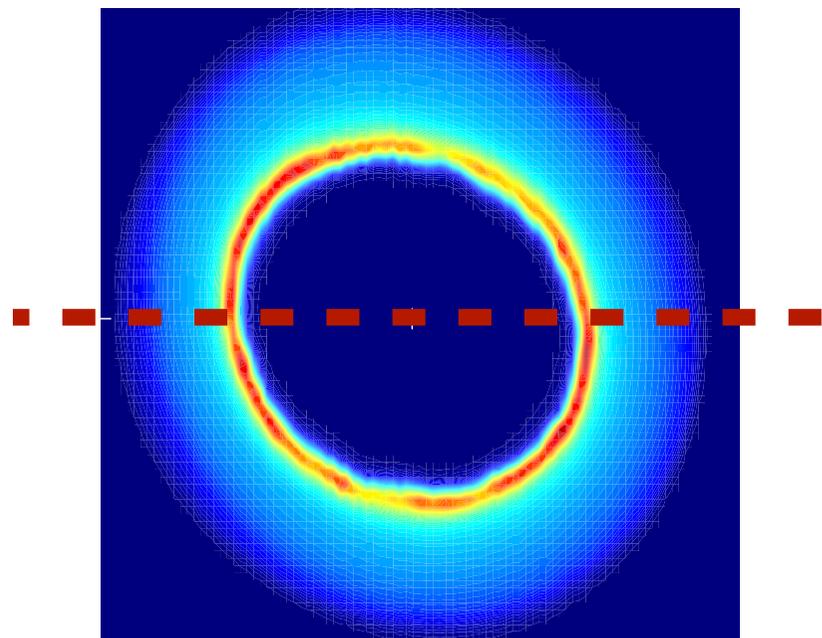
**radial  
profile**



passing from a flat  
current  
distribution...

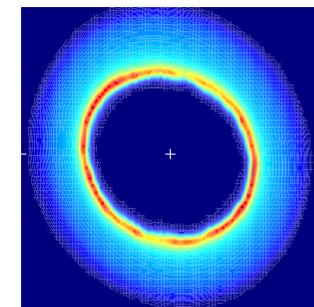


...to a more realistic distribution

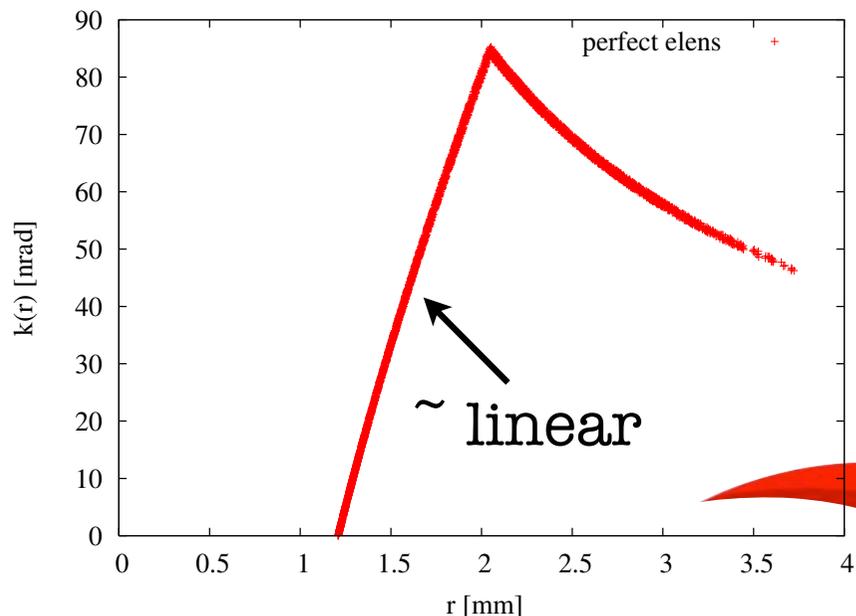




radial profile



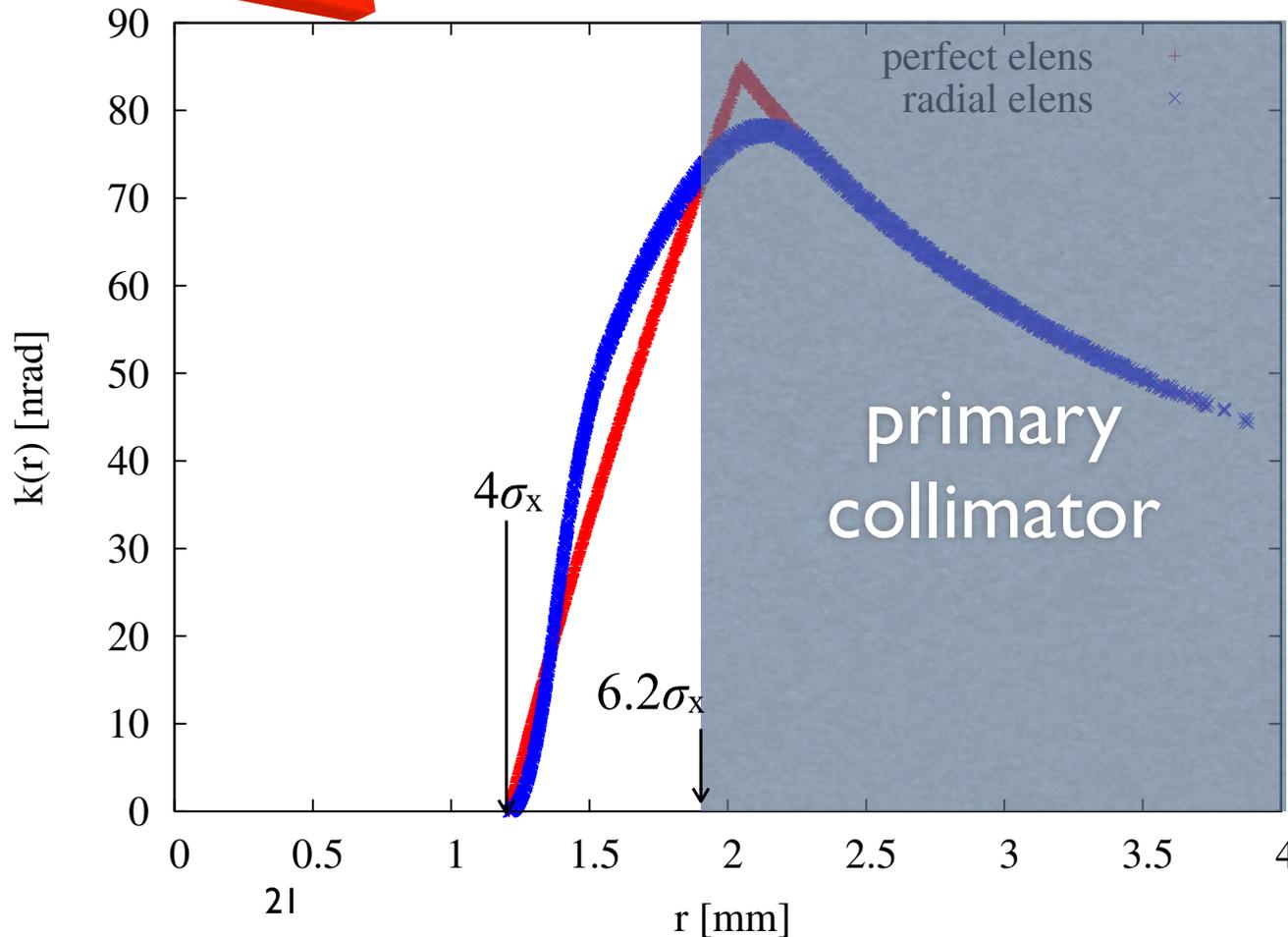
effect on the electric field



The effect on the integrated function is less evident.

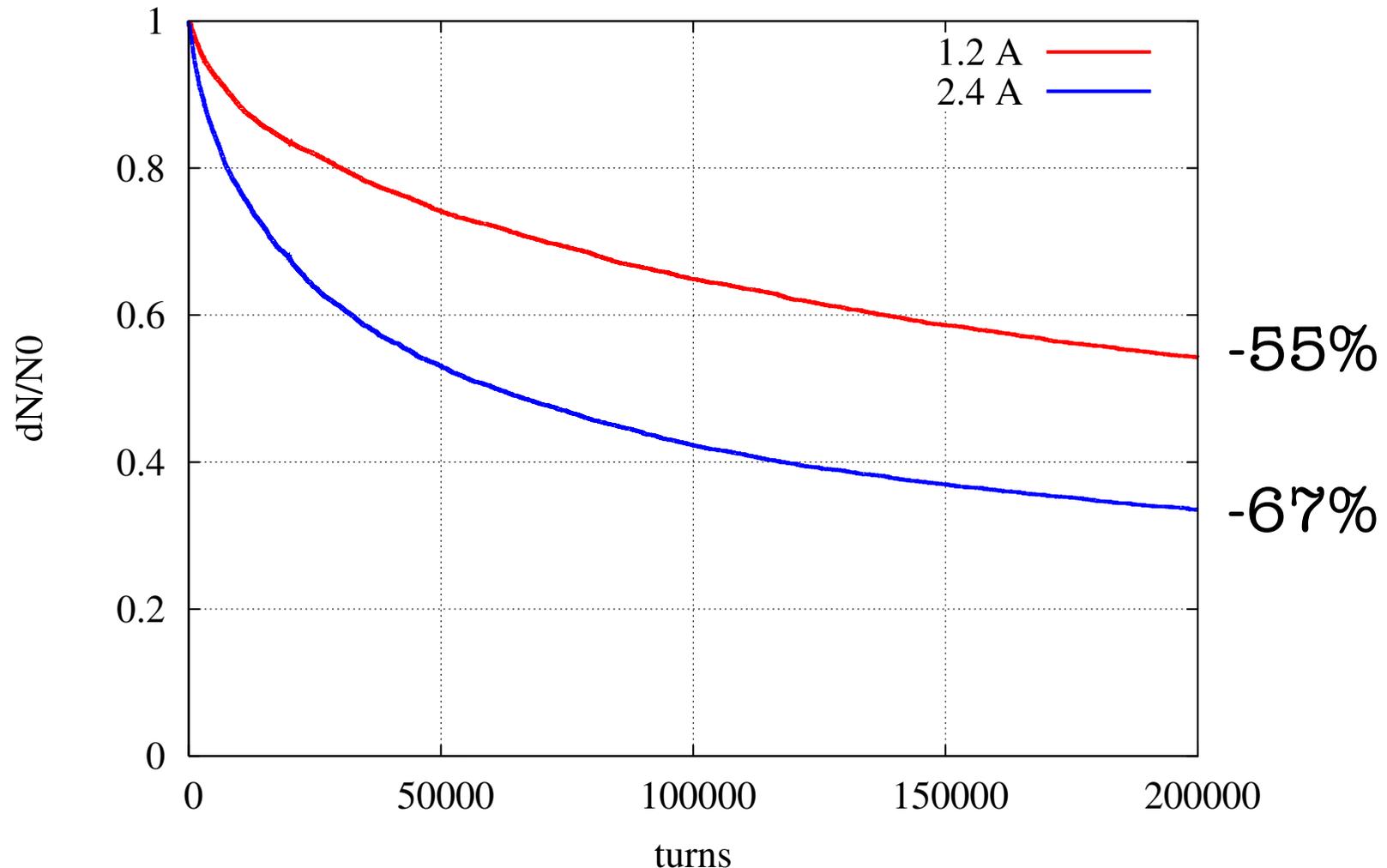
We get slightly larger kicks in the region between 4 and 6 sigma.

**An improvement of cleaning of about 10% is achieved for random and AC mode**



# can we tune the speed?

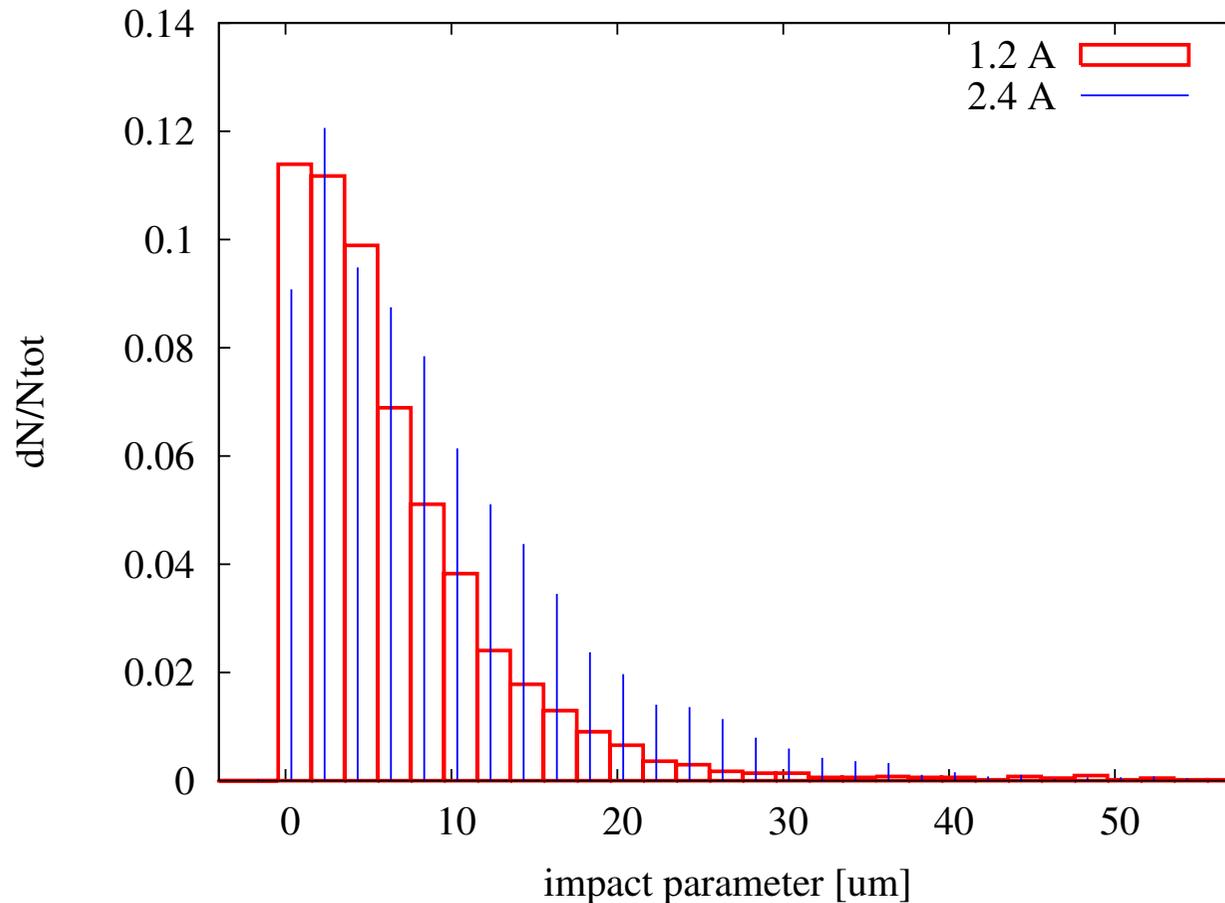
a current of 1.2 A is a conservative estimate. With the new cathode (ready) for the LHC we can easily reach higher values.



It is perfectly acceptable to assume that we can clean about 70% of the halo particles (from 4 to 6 sigma) in 20s

# any side effect?

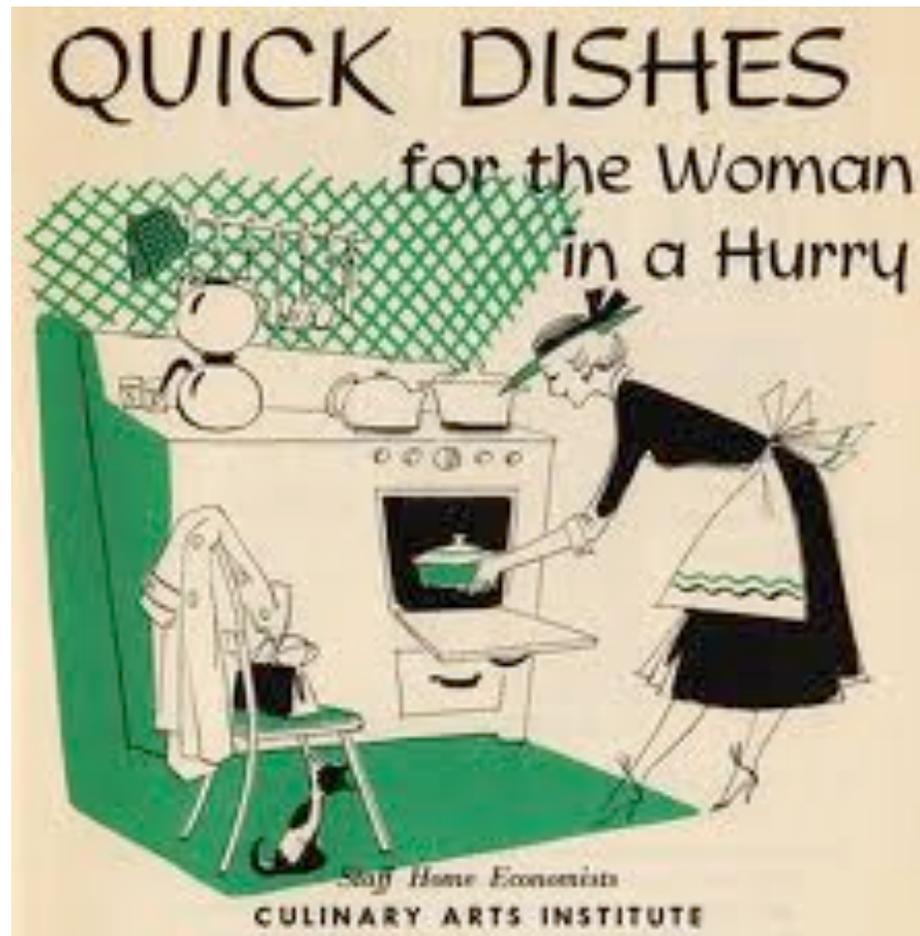
what happens to the scraped particles?



impact parameter  
on primary  
collimator.

the impact on primary collimator is about 10 times larger than the usual assumed values. According to past studies this should not affect the cleaning efficiency of the standard system, but it could **increase the crystal collimation efficiency.**

Long story short...



# Long story short...

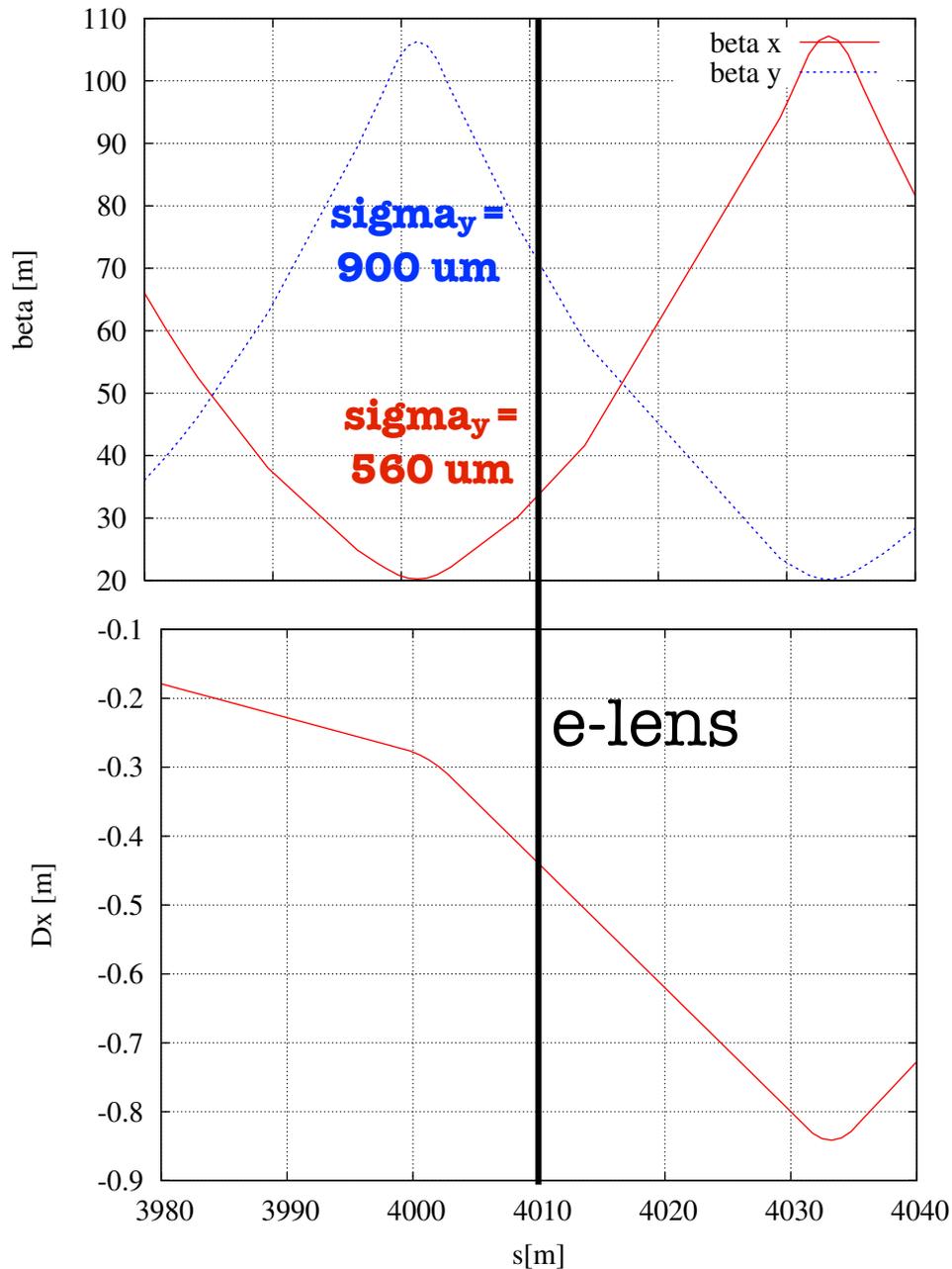
- The simulation of e-lens is an on-going work, however few important statements can be already done:
  - among the possible e-lens usage, the **random mode** seems to be the most robust and efficient for **fast scraping**
  - With relatively achievable e-lens currents, **more than 65% of the halo particles between 4 and 6 sigma can be lost in about 20 s.**
  - Many effects like natural diffusion, beam-beam, multipole errors (non included yet) are expected to enhance the electron lens effect.
  - In general, non linearities tends to increase the efficiency of the **DC mode as a slow scraper**. Already with octupoles a loss of **about 5%** is achieved in about 20 s.

# e-lens in the SPS?

Even if the physics case has been studied for the LHC, time/practical constraints could prevent us from an early installation of the e-lens in the LHC.

A possible alternative could be to perform the first beam tests in SPS. Does it make sense?

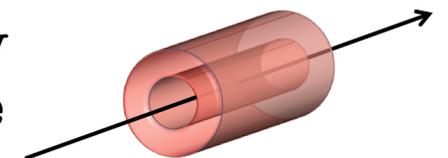
CONS	PROS
<ul style="list-style-type: none"><li>● cost of 270 GeV (~1/4 of Tevatron energy)</li><li>● Less instrumentation</li></ul>	<ul style="list-style-type: none"><li>✓ SPS is more similar to the LHC than Tevatron (proton machine, same LHC working point, weakly coupled...)</li><li>✓ reproduce Tevatron results at CERN</li><li>✓ validate simulation results</li><li>✓ acquiring experience with the object (cryogenics, vacuum)</li><li>✓ developing dedicated control software</li></ul>



collex location (LSS4).  
different beta function values  
 (  $H=30\text{m}$  vs  $V=76 \text{ m}$  )

Example: **inner radius at 2.7 mm**  
 scraping at **3  $\sigma_{y1}$**  VERT  
 scraping at **4.7  $\sigma_{x1}$**  HOR

scraping has been  
 simulated separately  
 in V and H, using the  
 same collimator  
 (changing its  
 orientation)



**Perfect e-lens,  
 linear machine**

the scraping will be mainly in the Vertical plane. Nowadays the LHC-type collimator is oriented in the horizontal plane.

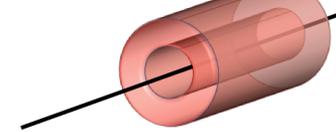
## CONS

- 1/4 of the TeV energy
- Less instrumentation
- Optimal layout would require a vertical collimator

a shift of 5 m would be already enough to solve the issue - and the space is available (see integration talk - Adriana)

## PROS

- ✓ SPS is more similar to the LHC than Tevatron (protons, same LHC working point, weakly coupled...)
- ✓ reproduce Tevatron results at CERN
- ✓ validate simulation results
- ✓ acquiring experience with the object (cryogenics, vacuum)
- ✓ developing dedicated control software



**Perfect e-lens,  
linear machine**

$$\theta(r) = \frac{2L f(r) I_T (1 \pm \beta_e \beta_p)}{4\pi\epsilon_0 r (B\rho)_p \beta_e \beta_p c^2}$$

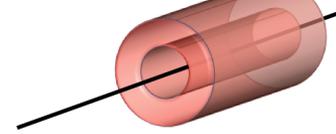
$$f(r) = \begin{cases} 0 & r < R_1 \\ \frac{r^2 - R_1^2}{R_2^2 - R_1^2} & R_1 < r < R_2 \\ 1 & r > R_2 \end{cases}$$

maximum kick for SPS case  $\sim 1 \mu\text{rad}$  (10x the LHC case)

For 270 GeV and normalized emittance of 3.5 mm mrad, this corresponds to about 5% of the sigma.

Removal rates in 200K turns (5 sec)

DC	AC	random
0%	(90% in 20 sec for the LHC) 91%	(42% in 20 sec for the LHC) 35%



**Perfect e-lens,  
linear machine**

$$\theta(r) = \frac{2L f(r) I_T (1 \pm \beta_e \beta_p)}{4\pi\epsilon_0 r (B\rho)_p \beta_e \beta_p c^2}$$

$$f(r) = \begin{cases} 0 & r < R_1 \\ \frac{r^2 - R_1^2}{R_2^2 - R_1^2} & R_1 < r < R_2 \\ 1 & r > R_2 \end{cases}$$

maximum kick for SPS case  $\sim 1 \mu\text{rad}$  (10x the LHC case)

For 270 GeV and normalized emittance of 3.5 mm mrad, this corresponds to about 5% of the sigma.

Removal rates in 200K turns (5 sec)

DC	AC	random
0%	(90% in 20 sec for the LHC) 91% ?	(42% in 20 sec for the LHC) 35%

to be verified with non linearities

Removal rates in 20 seconds 76%

CONS	PROS
<ul style="list-style-type: none"><li>● 1/4 of the TeV energy</li><li>● Less instrumentation</li><li>● Optimal layout would require a vertical collimator</li></ul> <p>a shift of 5 m would be already enough to solve the issue - and the space is available (see Adriana)</p>	<ul style="list-style-type: none"><li>✓ SPS is more similar to the LHC than Tevatron (protons, same LHC working point, weakly coupled...)</li><li>✓ reproduce Tevatron results at CERN</li><li>✓ validate simulation results</li><li>✓ acquiring experience with the object (cryogenics, vacuum)</li><li>✓ developing dedicated control software</li><li>✓ The e-lens operation is identical to the LHC case, the timescale of the effects is only a factor 4 different</li></ul> <p>all prototypes for the LHC collimation system have been tested in SPS: experience has been always precious</p>

Recently an operational use of the device in SPS was also suggested:

# e-lens as a scraper in SPS?

following discussions with S. Redaelli, B. Salvachua Ferrando, A. Rossi

modifications of the layout are probably required

1. Integration for beam test (add collimators? both planes?)
2. Minimum duration of excitation to have effective scraping (can we do it in short times before extraction?)
3. Can we change the size of the hole to match the variation of beam size during the ramp?

likely, but still have to be addressed in details

# e-lens in the SPS?

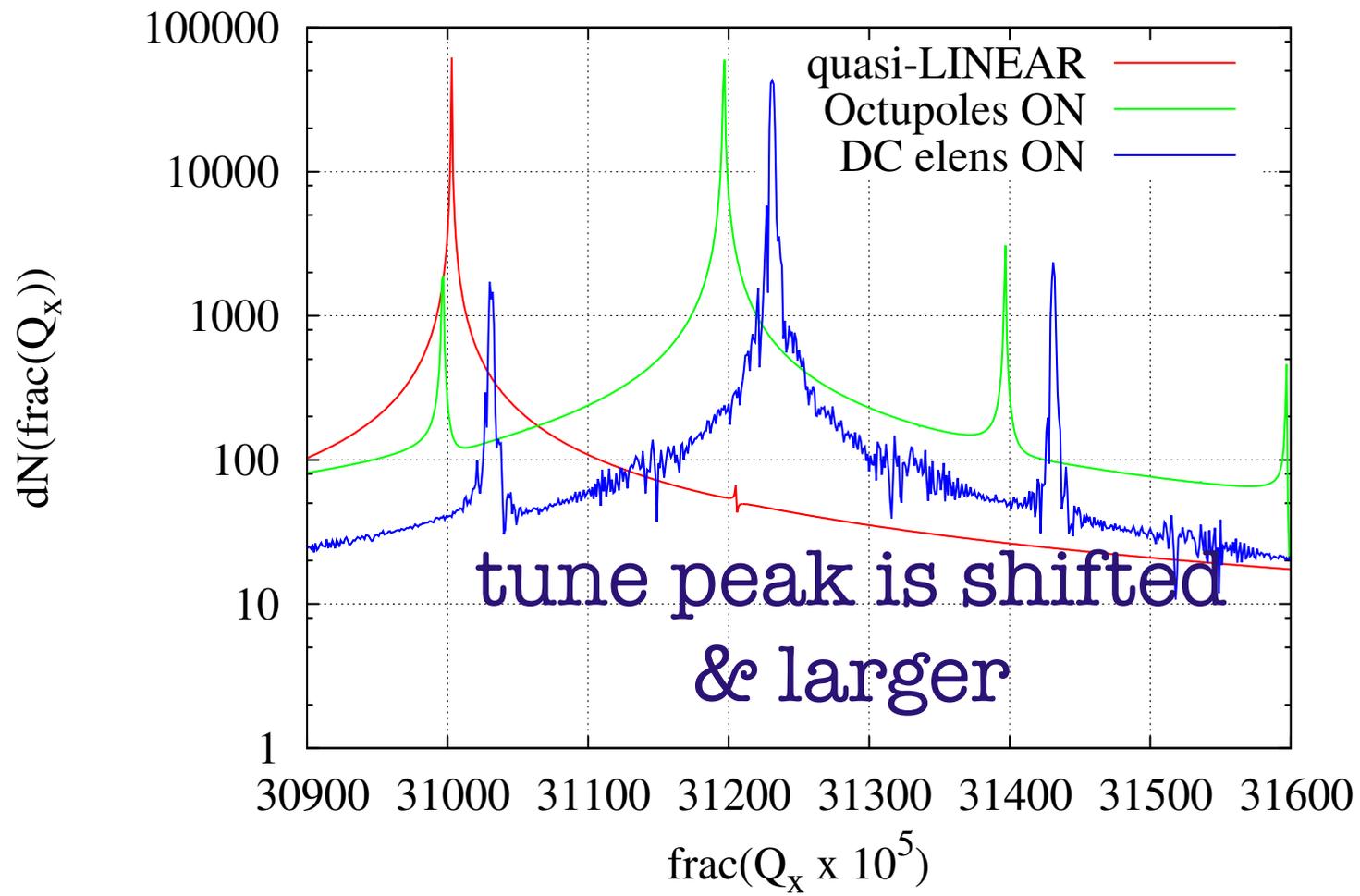
## summary

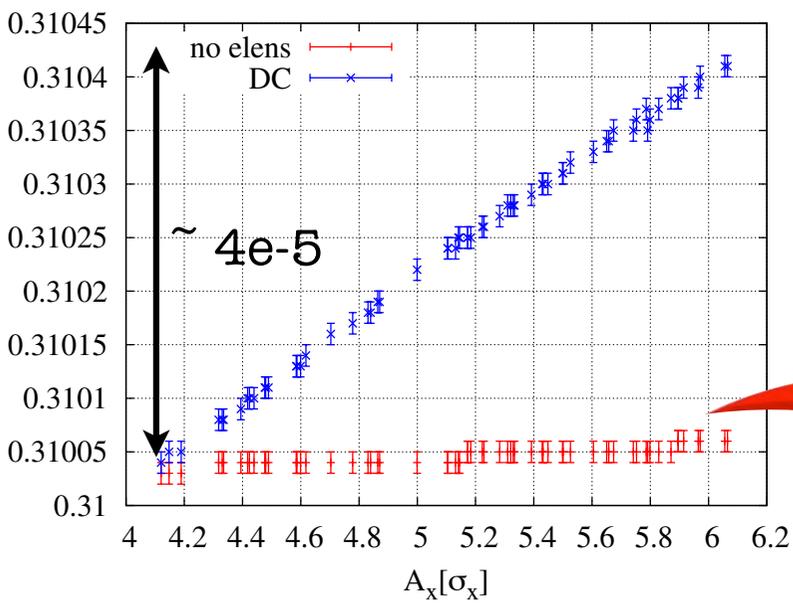
- SPS has been simulated with Sixtrack, using the linear machine and the perfect e-lens model
- Results for the LHC have been qualitatively confirmed in the SPS
- **From the simulations at 270 GeV it is clear that the current e-lens can be used for meaningful beam studies**
- The only shoe-stopper could be the required modification of the layout - but this can be solved if we shift the device of 5-6 m
- The usage of the current e-lens as an operative device is likely, but further investigations and possible hardware modifications will be required.



special thanks to  
Riccardo de Maria, Guido Sterbini, and the  
whole collimation team for the useful  
discussions.







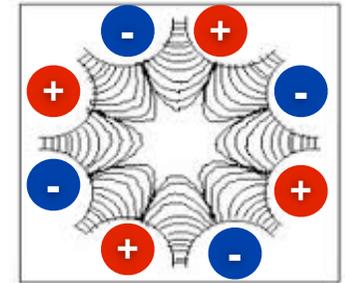
purely H halo, quasi-linear machine

For each frequency there is a narrow, well defined tune

Total tune range  $\sim 4e-5$



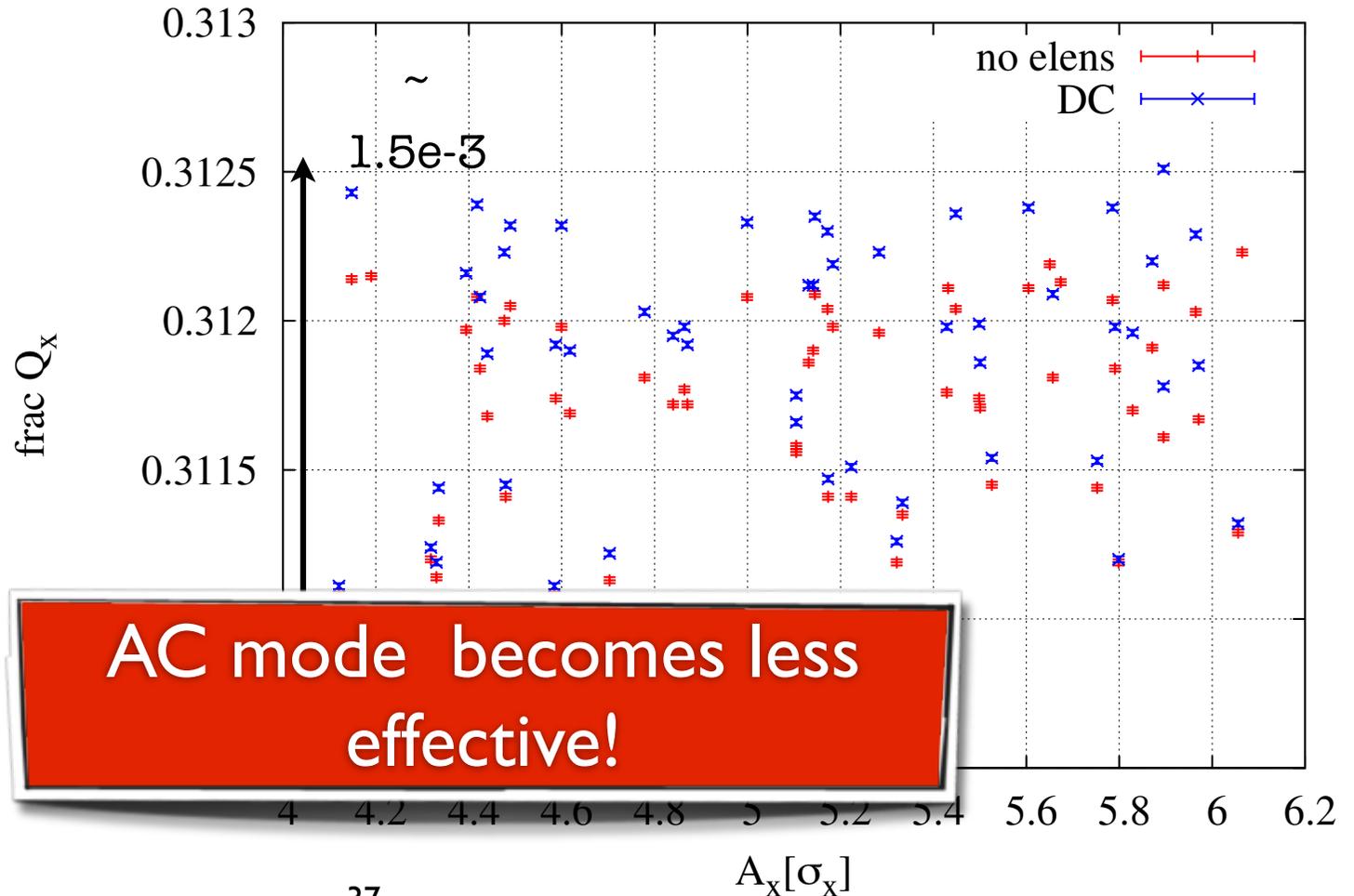
**non linearities (octupoles)**



3D distribution + octupoles

Tune peaks are larger  
→ **difficult to keep particle in a resonance**

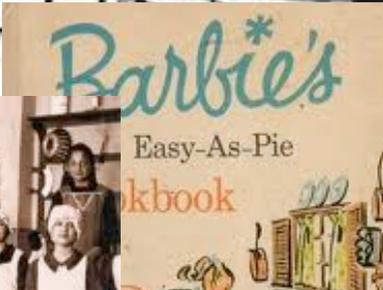
Total tune range  $\sim 1.5e-3$   
→ **covering all the interesting tunes takes more time!**



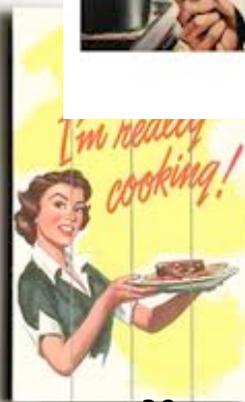
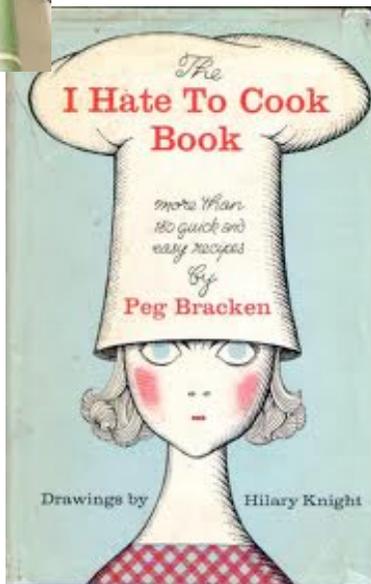
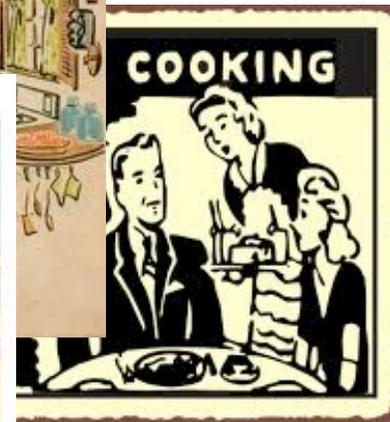
**AC mode becomes less effective!**



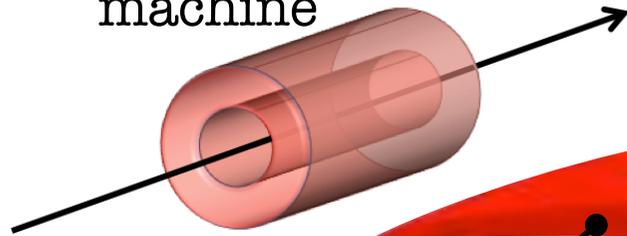
Reproduction rights obtainable from:  
[www.CartoonStock.com](http://www.CartoonStock.com)



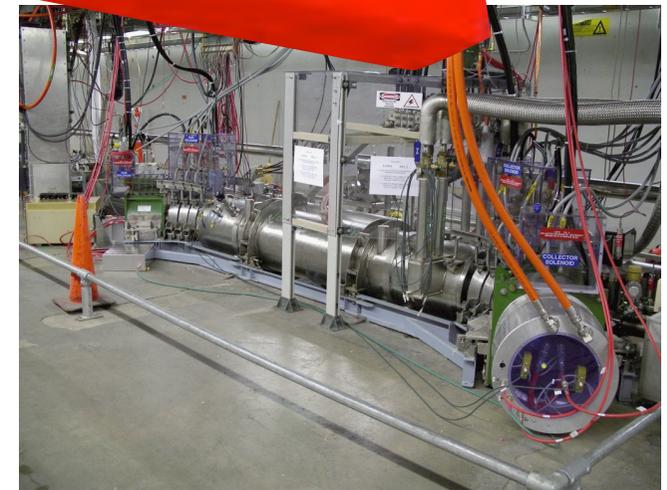
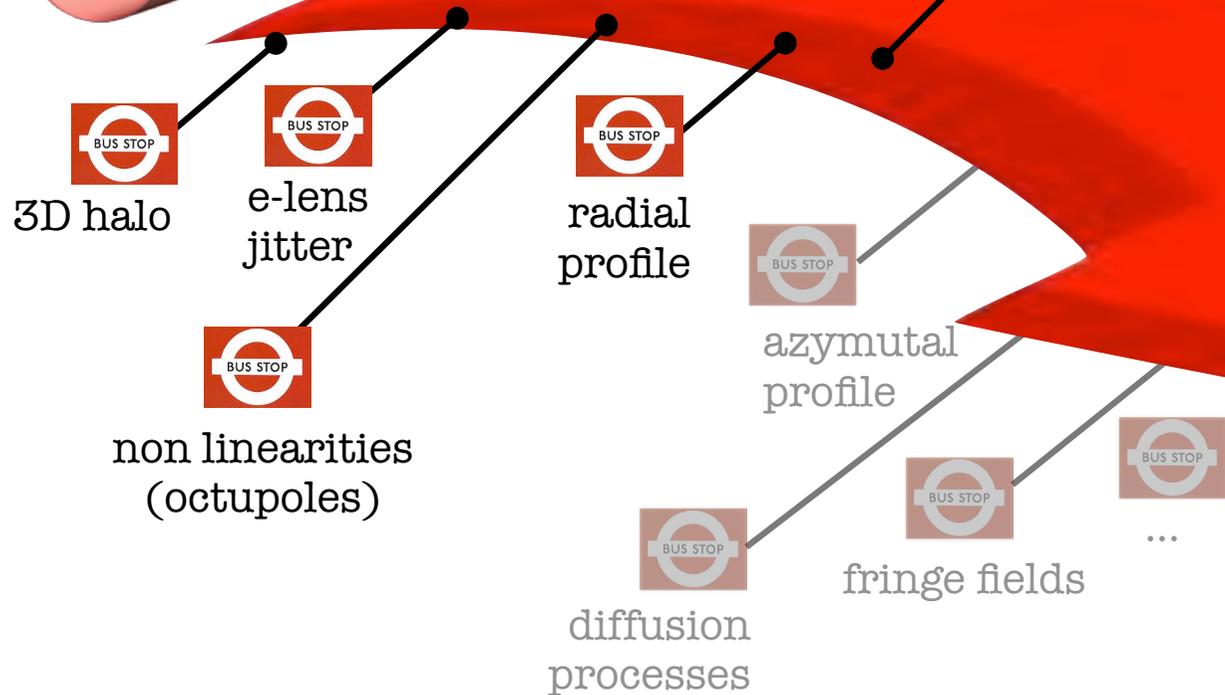
INTO A BAKING DISH



Perfect e-lens in  
quasi-linear  
machine



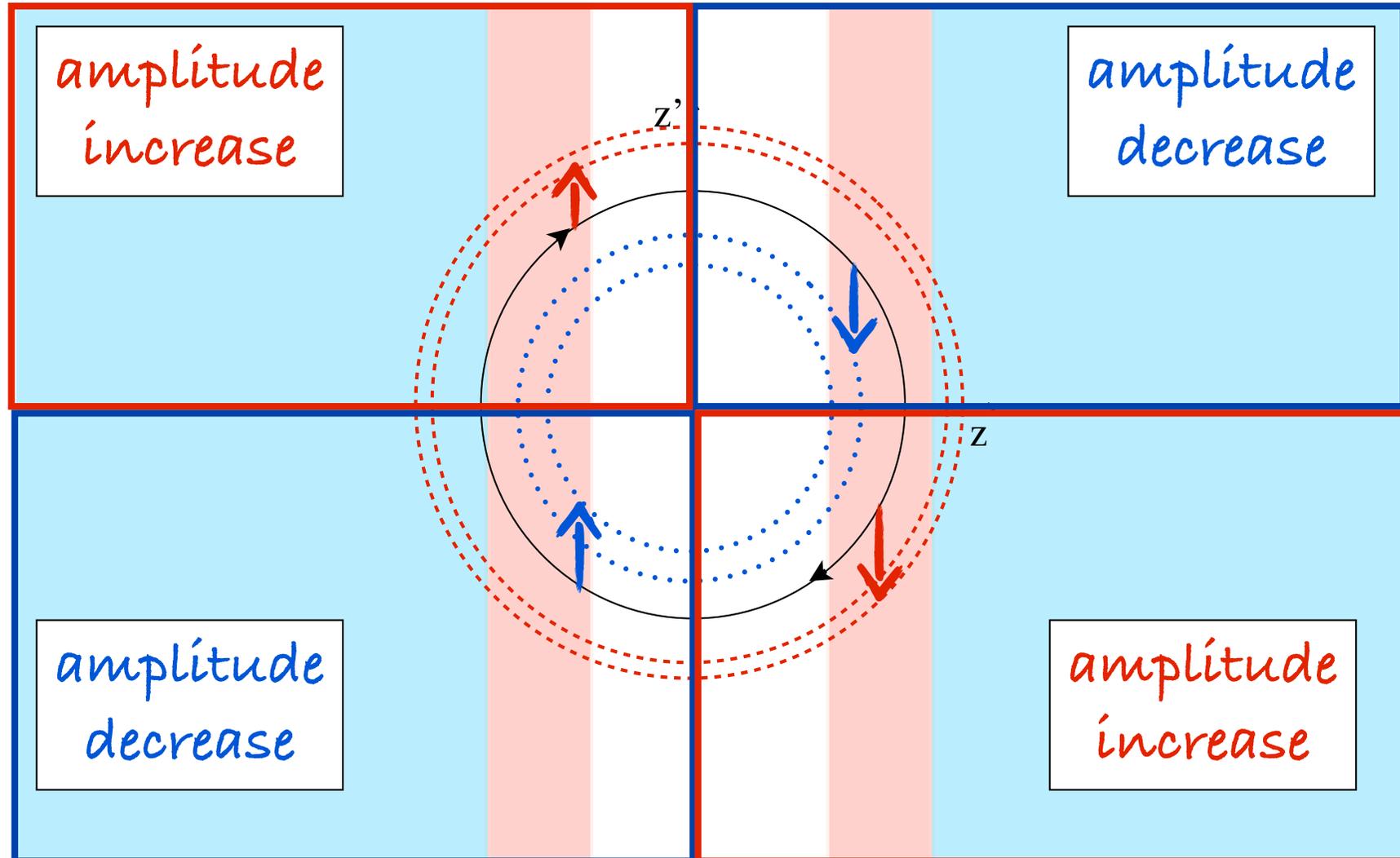
Today!



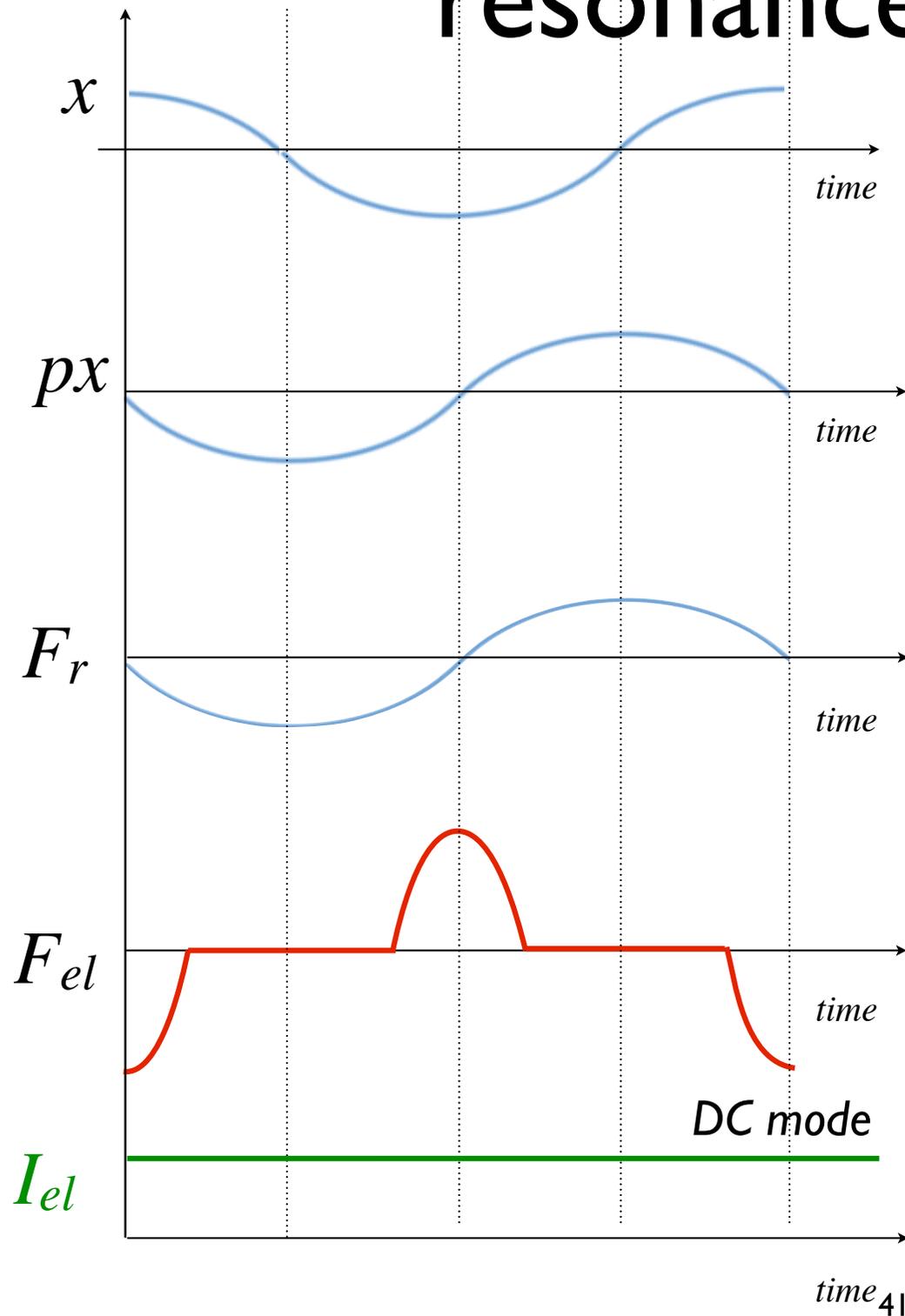
Real e-lens in real machine

It's a long way, which requires  
many intermediate stops

# (normalized) phase space



# resonance mode

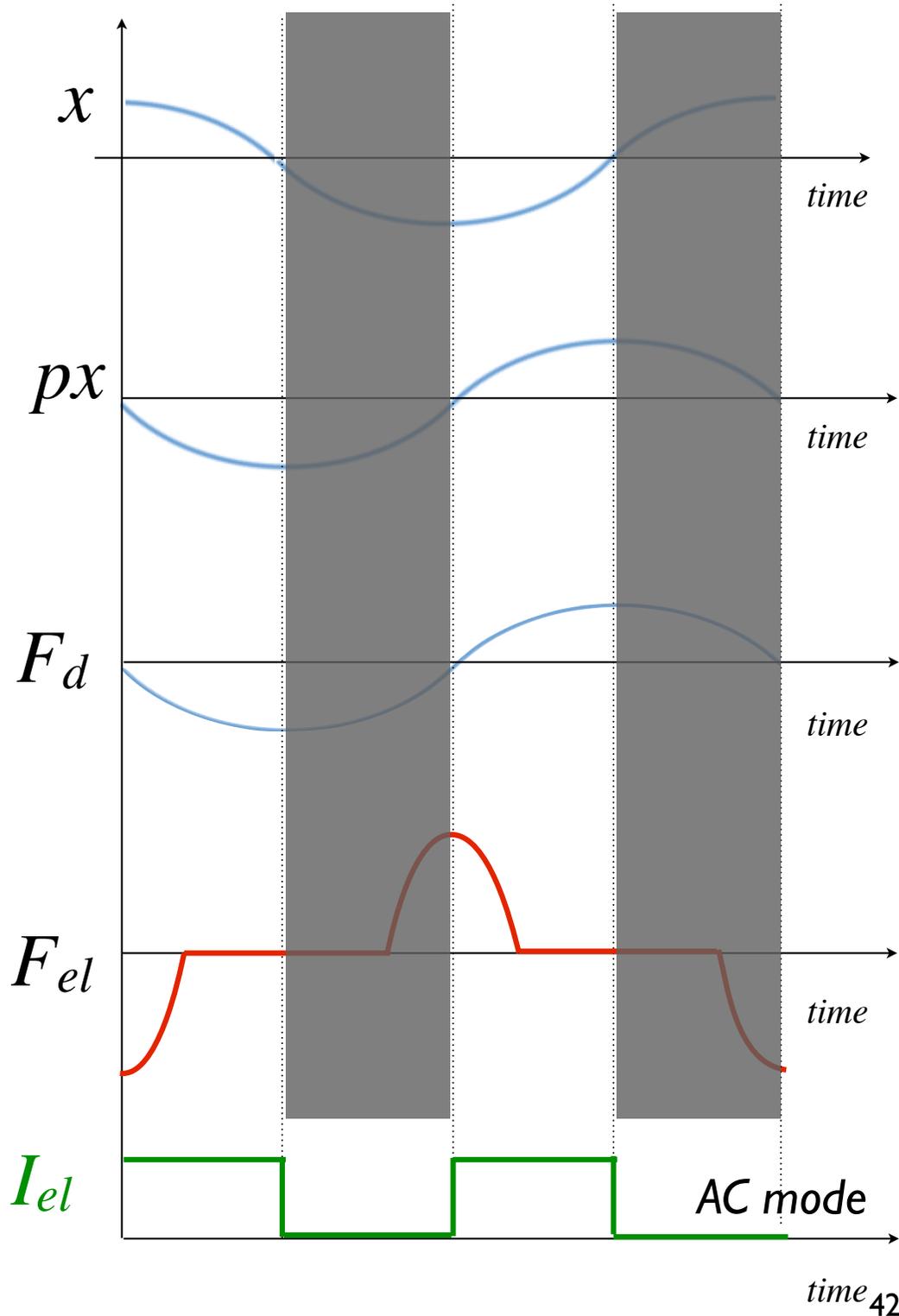


taking a particle with initial phase = 0

this is its its momentum

the resonant force which acts on this particle must be in phase with the momentum, and with the same oscillation period

the electron lens is proportional to the particle position => ALWAYS shifted in phase (90 degrees) with respect with the particle momentum



taking a particle with initial phase = 0

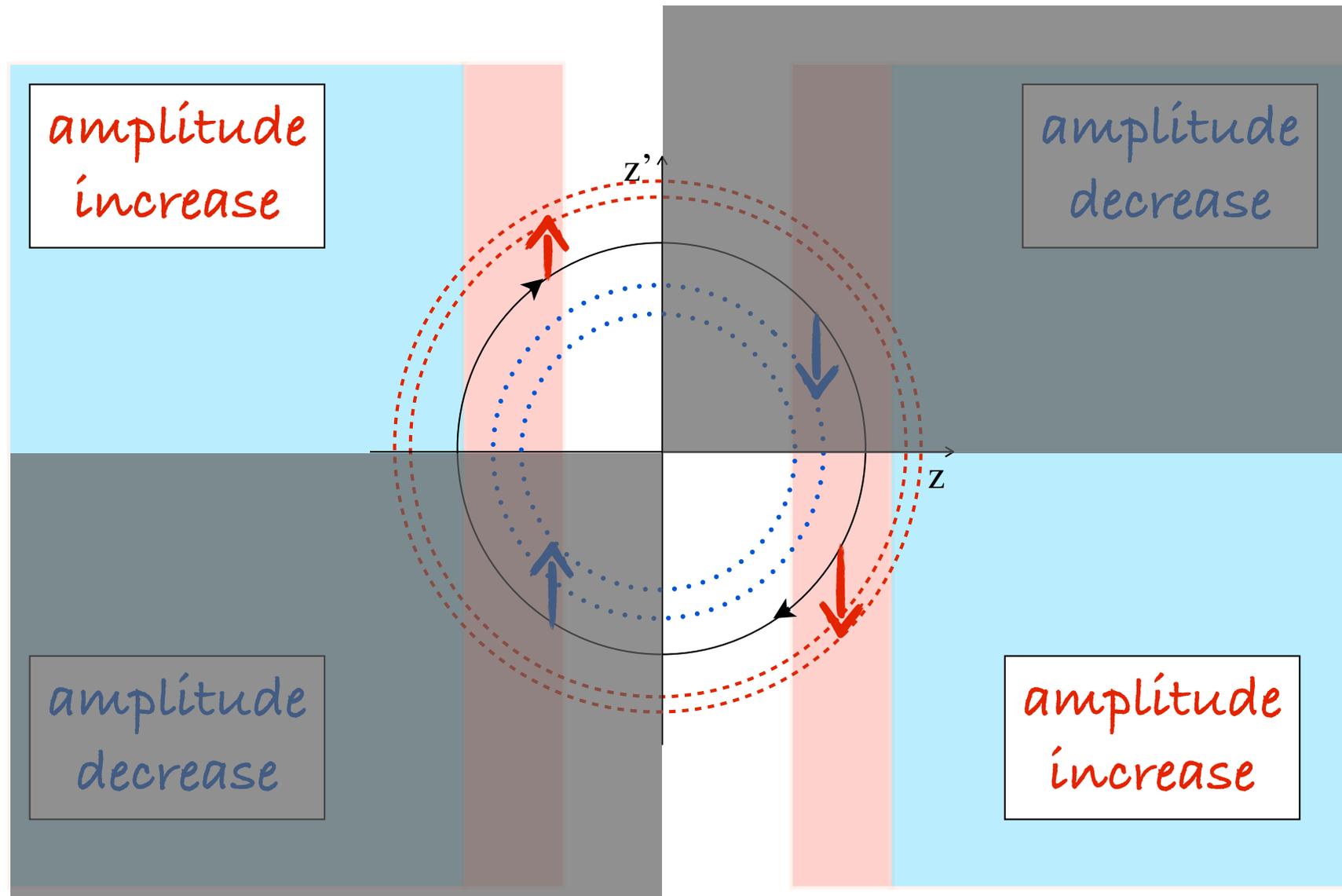
this is its its momentum

the resonance driving force which acts on this particle must be in phase with the momentum, and with the same oscillation period

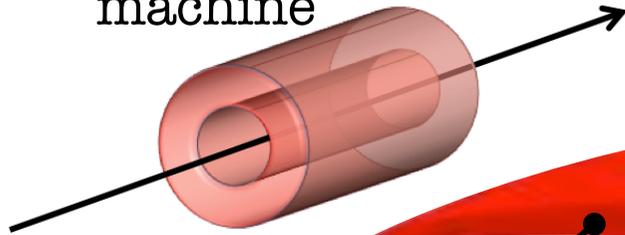
the electron lens is proportional to the particle position => ALWAYS shifted in phase (90 degrees) with respect with the particle momentum

Resonant condition:  
 I switch the ELENS on only when it gives a kick in the same direction as xp

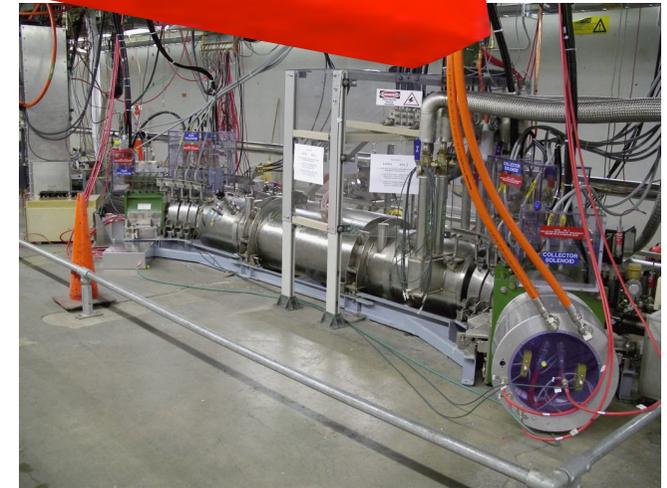
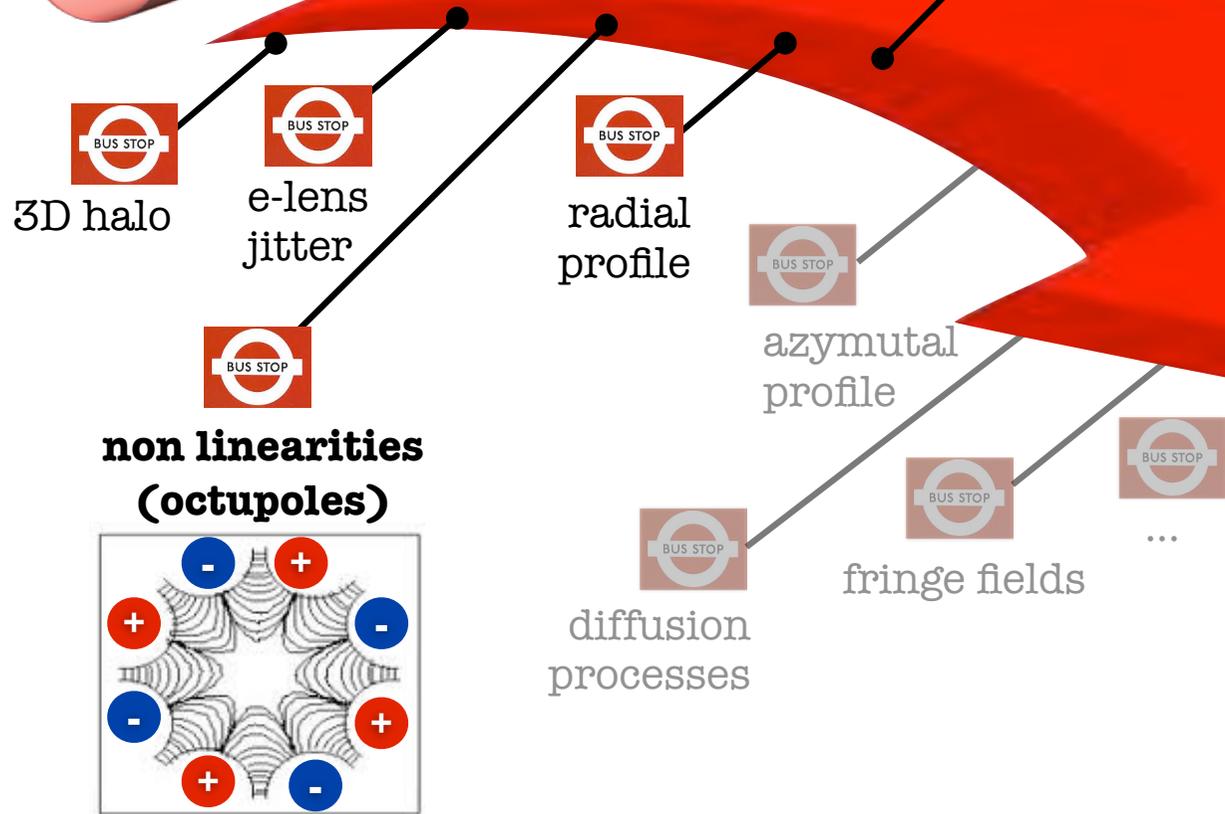
# (normalized) phase space



Perfect e-lens in  
quasi-linear  
machine

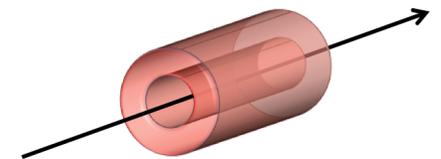


Today!



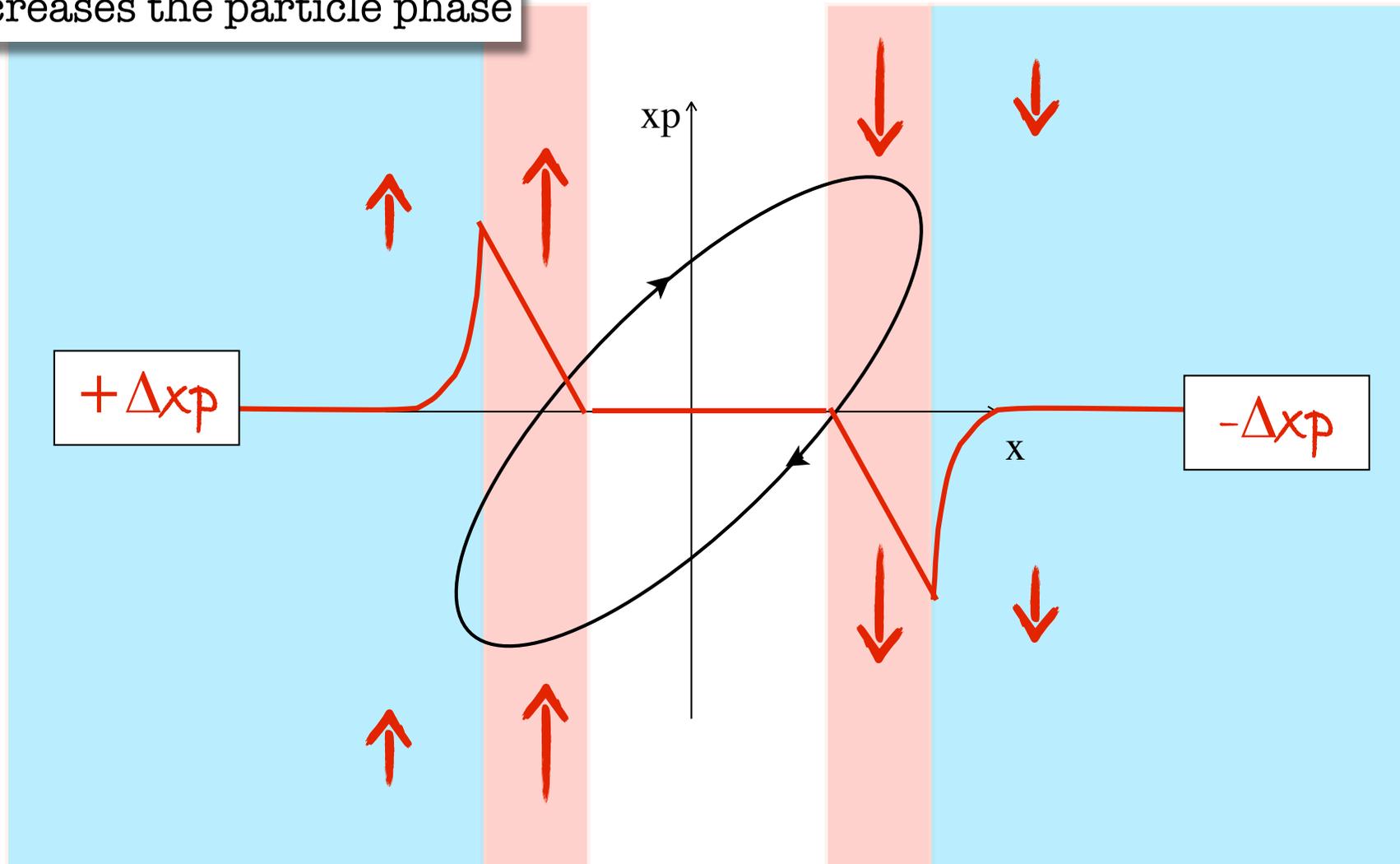
Real e-lens in real machine

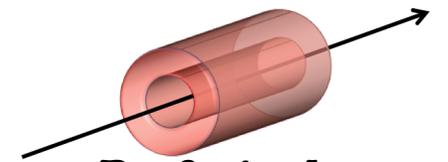
# The perfect e-lens: the nominal kick



**Perfect e-lens,  
linear machine**

the kick is focussing  
⇒ always inward  
⇒ increases the particle phase

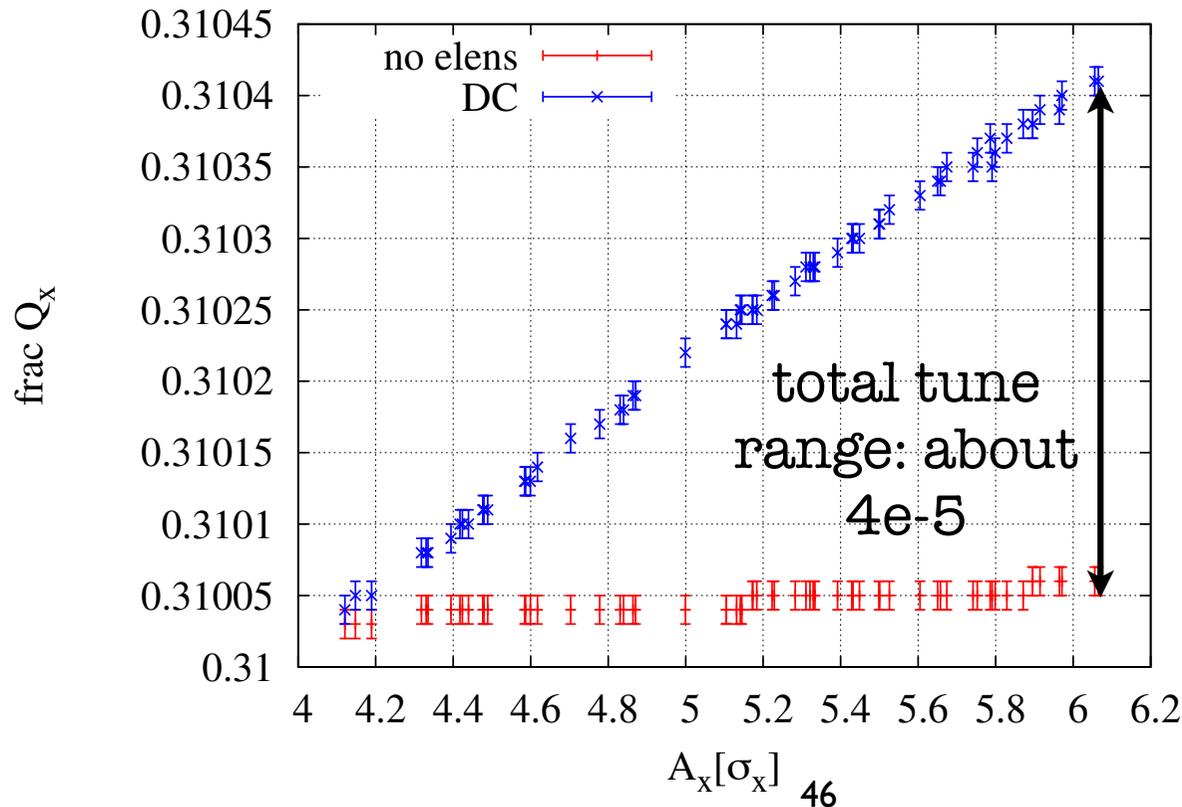




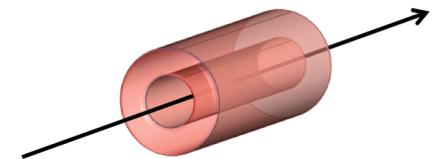
Perfect e-lens,  
linear machine

## 2. *AC mode*: e-lens switched on-off in resonance with the betatron tune

*which tune?*

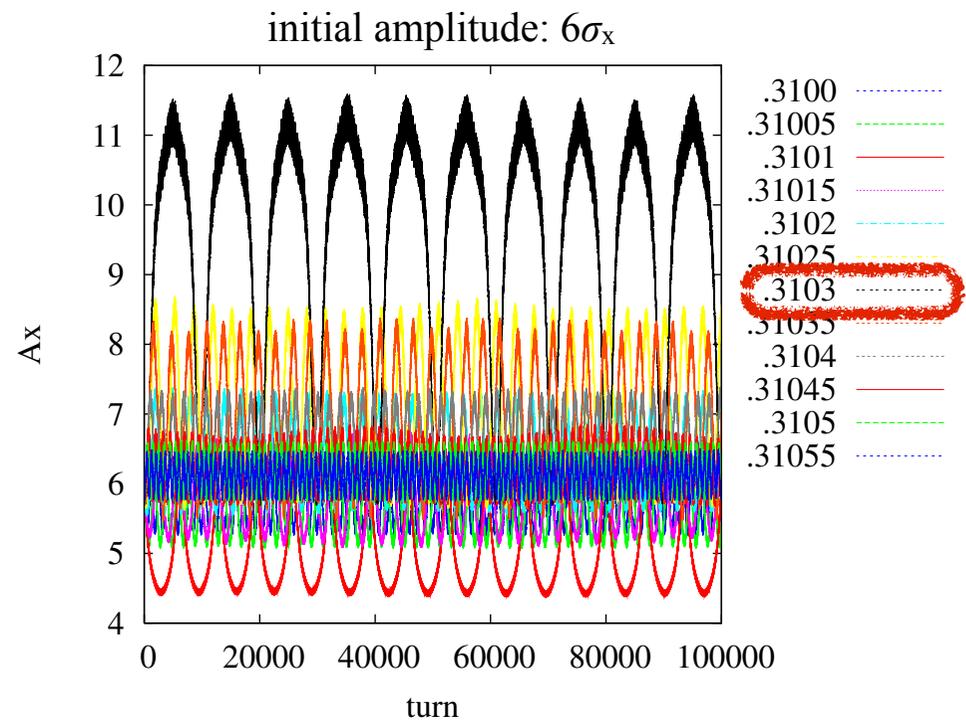
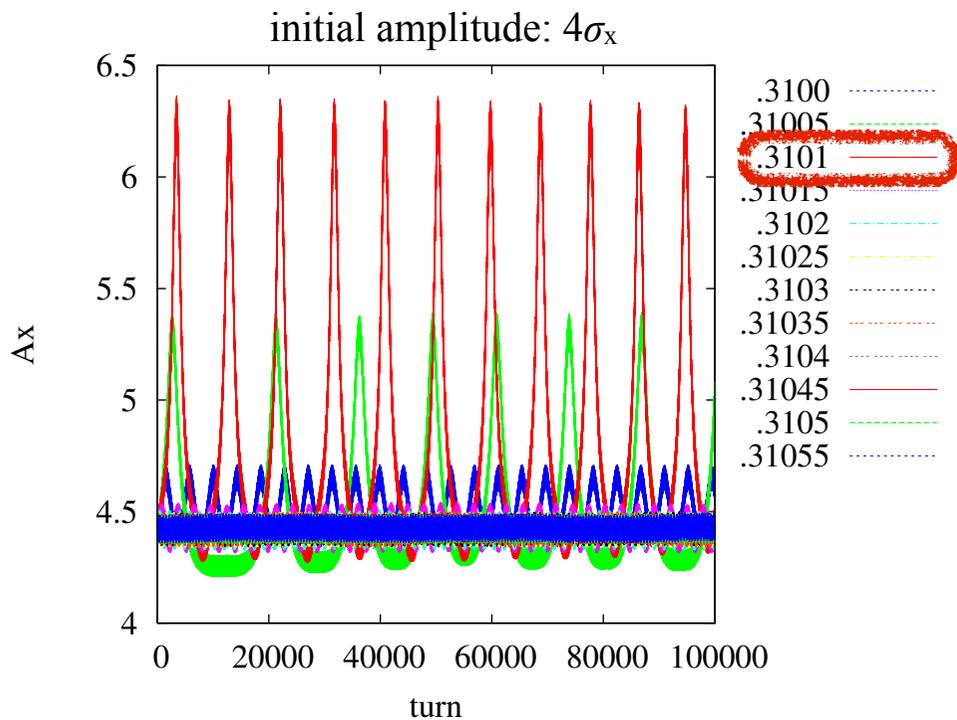


the e-lens itself introduces a tune shift, so that different (amplitude) particles have different tunes



Perfect e-lens,  
linear machine

## 2. *AC mode*: e-lens switched on-off in resonance with the betatron tune



... it follows that different (amplitude) particles respond to different excitation frequencies